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Measuring Round Trip Times to Determine the Distance between WLAN Nodes

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Abstract

This technical report explores the degree of accuracy to which the propagation delay of WLAN packets can be measured using today's commercial, inexpensive equipment. The aim is to determine the distance between two wireless nodes for location sensing applications. We conducted experiments and measured the time difference between sending a data packet and receiving the corresponding immediate acknowledgement. We found the propagation delays correlate closely with the distance, having only a measurement error of a few meters. Furthermore, they are more precise than the received signal strength indications.

To overcome the low time resolution of the given hardware timers, various statistical methods are applied, developed and analyzed. For example, we take advantage of drifting clocks to determine propagation delays that are forty times smaller than the clocks' quantization resolution. Our approach also determines the frequency offset between remote and local crystal clocks.

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Introduction

Knowing the distance between wireless nodes is required for location-aware services and applications. The distance helps to calculate the position of wireless nodes, to decide the time of handovers, or to find the optimal routing path throughout an ad-hoc network.

A couple of approaches for in- and outdoor location sensing techniques have been presented [1]. In this paper we focus on locating techniques which use the intrinsic features of WIFI based wireless access. The RADAR system [2] has been one of the first approaches presenting an indoor positing system based on WLAN components – others have followed ([3–9] and the references therein). An essential part of location sensing algorithms is a method to determine the distance between two wireless nodes. In general, three methods have been considered:

- 1. The information, which nodes are within transmission range, is used to estimate the distance. This approach benefits from densely populated networks such as sensor networks [10].
- 2. The received signal strength indication (RSSI) of data packets is considered as it decays with distance. Actually, the RADAR system and most other proposals are based on RSSI. Because RSSI decreases sharply in a non-linear fashion with distance, signal strength maps have to be gathered to relate the RSSI values with positions. Generating these maps is time-consuming and it has to be redone if the environment changes.
- 3. The propagation time of radio signals can be used because in free air it linearly increases with the distance. Such an approach is usually considered to be impossible without the help of special signal processing hardware [11].

In this paper we show that precise location positioning based on round trip time measurements of WLAN packets is indeed possible even with low-cost, commercial WLAN hardware. We developed the algorithms to determine indirectly the air propagation time and to improve the accuracy and resolution of the time measurements. We validated our approach with two independent experimental measurement campaigns and with an analytical explanation.

We take advantage of an intrinsic feature of IEEE 802.11: Each data packet is immediately acknowledged by its receiver (Figure 1.1). We measure the time between starting the transmission of a data packet and receiving the corresponding immediate acknowledgement. We will refer to this as remote delay (t_{remote}). We also measure the duration of receiving one data packet and sending out the



Figure 1.1: Distance Measurement: ICMP Ping sequence diagram.

immediate acknowledgement. We will call this duration local delay (t_{local}) . The overall propagation time is then estimated by subtracting the local time from the remote delay (1.1).

$$c = \frac{2 \cdot distance}{t_{remote} - t_{local}}$$
where $c \approx 3 \cdot 10^8 \frac{\text{m}}{\text{s}}$ being the speed of light. (1.1)

The most difficult part of this work was to cope with the low resolution of the clocks: If the operating system records the time stamps of outgoing and incoming packets, the variable interrupt latency falsifies the results. Most WLAN solutions allow to record time stamps at a resolution of 1 μ s. However, packets travel a distance of 300 m in 1 μ s, which usually exceeds the range of WLAN transmission. We achieve a more precise resolution by using multiple delay observations and applying statistical methods to enhance the accuracy.

We take advantage of the fact that both local and remote clocks are drifting and interfere. The interference is caused by the data-acknowledgement sequence. As a result the observations contain a beat frequency that is equal to the frequency offset of local and remote clock crystals. The beat frequency introduces measurement noise, which we utilize to identify a weak signal below the timers' quantization resolution. The weak signal is the propagation delay.

This paper is structured as follows: In chapter 2 we refer to the state of the art. Then we explain our approaches to enhance the measurement resolution. In chapter 4 and 5 we describe our experimental measurement campaigns. Finally, we briefly summarize the results and contributions of this paper.

Related Work

In the realm of Information Technology, the classic approach estimates the time of arrival (TOA) of pure radio signals (instead of WLAN packets) for position location purposes. This is conducted by applying signal processing algorithms based on cross-correlation techniques [12]. The received signal resembles the initial transmitted signal delayed by propagation delay. The autocorrelation function for the transmitted signal accounting shows its maximum peak for a certain shift in time (τ = time lag). TOA based time measurements require synchronised clocks. Although TOA as a ranging metric is considered to be the most popular technique for accurate indoor positioning [13], the method suffers from multi-path conditions. The difficulty is to determine the autocorrelation peak referring to signal travelling along the direct line of sight (DLOS). The problem can be encountered with a wider frequency band, e.g. ultra-wide band.

TOA measurement is being employed both outdoors for GPS-positioning [14] and indoors to find things and people marked by a tag [15]. In the latter paper, the author gives an appraisal of the achievable accuracy when measuring the round trip TOA within the 2.44 GHz and 5.78 GHz bands. For a signal bandwidth of 40 MHz, the accuracy of 3.8 m can be an achievable resolution limit unless further signal processing techniques are applied. Those might enhance the resolution up to 1 m.

The only paper focussing on measuring pure packet propagation delays is [16]. It has actually inspired this work. The objective is to determine the speed of light using the averaged measured round trip propagation delay of many ping packets and the known distance between the sender and receiver. The measurements were conducted in a wired Ethernet infrastructure. Estimating the propagation delay which ranges below the clock resolution was facilitated by employing the concept of noise-assisted sub-threshold signal detection. The aim of this work is to teach students the effect of stochastic resonance [17] and to explain how to enhance the resolution. For measurements in an IEEE 802.11b wireless environment the round trip times were too variable and noisy to be used.

Approach

The presented approach is based on the ideas of [16]. We use the round trip time delay of packets to determine the distance as given in (1.1). In order to further enhance the measurement resolution, we utilize the IEEE 802.11 data/acknowledgement sequence instead of the ICMP-Ping request/response packet sequence. Also, we measure the time stamps not in the operating systems but on the WLAN card, which is not subject to variable interrupt latencies. Let us explain these enhancements:

The ping response is generated by operation systems and thus subject to a highly variable delay. In contrast, the immediate acknowledgements are handled by the hardware of the WLAN radio and highly predictable: On standardized IEEE 802.11 the MAC processing time (SIFS interval) is 10 μ s (802.11b) or 16 μ s (802.11a) with a tolerance up ±25 ppm resp. ±20 ppm. Acknowledgements are valid only if they are received after the SIFS interval with a tolerance of ±2 μ s resp. ±0.9 μ s. Thus, if the WLAN card is implemented according to the standard, the transmission delays are highly deterministic. We can also assume that the MAC processing times on both nodes are identical. However, in this paper, we will prove that not all WLAN cards operate in compliance with the standard.

Ping round trip times are measured in the operating system's kernel, for example during an interrupt. In [18] we showed that OS time measurements are quite imprecise due to variable interrupt latency. In our experiments, about 5% of the time stamps have an error of more than 2 ms. Also, in our experiments OS time measurements did not work if applied for distance measurements. Instead, we utilized the WLAN cards to record the transmission and arrival times of packets. These time measurements are not falsified by interrupt latency, because they are conducted by the hardware. The resolution of these hardware time stamps implemented in most current WLAN products is 1 μ s, which is still not precise enough because it is equal to 300 m.

The accuracy of delay measurements is hampered by a discrete time resolution. The resolution increases with multiple observations being combined and smoothened. This has the drawback that the determination of changes over time – e.g. due to node movement – is slower. In the following we discuss, which phenomena are considered to achieve a higher resolution using the mean of multiple observations.

3.1 Gaussian noise

The presence of measurement noise is assumed. Thus, the delay values are not limited to only one value. (In Figure 3.1 not only 323 μ s can be observed but also other values). If one assumes a



Figure 3.1: Discrete distribution of noisy delay measurements.

Gaussian noise distribution with a suitable strength, we can simply take the sample mean to enhance the resolution [19]. Also, it can be expected that different discrete delay values occur entirely random.

But which effects introduce noise? The measurement noise can be caused by thermal noise present in the received radio signal. Thus, the synchronization to the modulation symbols might vary. In the presence of a multi-path environment, the dominant propagation path might vary leading changes in the propagation delay. Also, the crystal clocks of the WLAN equipment are subject to a constant clock drift and variable clock noise.

3.2 Stochastic Resonance

Instead of the explanation above the authors of [16] suggested another statistic effect called stochastic resonance. The concept of stochastic resonance was originally introduced as an explanation for the periodically recurrent ice ages. In the last two decades, it has been applied to explain many physical phenomena [17, 20]. In the realm of signal detecting [21] stochastic resonance allows for detecting signals below the resolution of the measuring units because the signal becomes detectable with the help of noise. Noise adds to the signal so that it eventually exceeds the threshold given by the resolution of the detecting device.

For example, in a bi-stable system a state change occurs only if the weak signal added to the noise signal is higher than a barrier between both states. The length of the period that the system stays in one state is random. If one measures discrete values, the probability is high, that one value remains the same for the next observation. This effect results in blocks of the same values and these blocks have random lengths.

3.3 Beat Frequencies

In our experiments (Figure 4.3) it can be observed that the occurrence of 323 and 324 values occur in block of regular patterns. But this effect cannot be explained with the effect of stochastic resonance.

Another effect can also entail resolution enhancement even if measurement noise is missing: Both WLAN cards are driven by built-in crystal oscillators that have nearly the same frequency. Due to tolerances, there is a slight drift between both clocks. If two frequencies interfere, a so called beat frequency is produced. The beat frequency is the difference of both frequencies.

$$f_{beat} = |f_1 - f_2| \tag{3.1}$$

Let us consider the impact of discrete time resolution on the measurement error. First, we construct a model of the experiment setups. Instead of using packets we assume that a delta pulse is sent from the local to the remote node. After the delta pulse's arrival another delta pulse is sent from the remote to the local node representing an acknowledgement. The local node can process the impulses only in discrete time steps $loc \in \mathbf{N}$ described with natural numbers. The remote node also reacts only in discrete time steps, which are $rem = \delta + n$ where $n \in \mathbf{N}$ and phase offset of $\delta \in [0; 1[$. We assume that the clocks work at the same speed but a phase offset is present. The phase offset changes over time but not for the duration of a round trip. The transmission of a delta impulse from one node to the other takes the time of $dist \in \mathbf{R}^+$, which is equal to the propagation time.

Let us assume that a delta impulse is sent out from the local node at time loc_{out} . It arrives at the remote node dist times later. Due to the discrete MAC processing, the delta impulse is only identified at the next clock impulse, which is:

$$rem = \left[(loc_{out} + dist) - \delta \right] + \delta \tag{3.2}$$

At the same time, the remote node sends back a delta impulse representing the acknowledgement. It arrives at the local node *dist* times later, but is again recognized only at the next clock, which is

$$loc_{in} = \lceil rem + dist \rceil \tag{3.3}$$

Then, the observed round trip time rtt is (3.4). It is display in Figure 3.2.

$$rtt = loc_{in} - loc_{out}$$

= $\left[\left[loc_{out} + dist - \delta \right] + \delta + dist \right] - loc_{out}$
= $\left[dist + \delta \right] + \left[dist - \delta \right]$ (3.4)

Next, we assume that the phase changes during the measurement. The change is constant and repeats after each phase period starting at zero again. In the following, we only consider one phase period and assume that round trip times are measured at all times. Thus, the number of observations is infinite. The mean rtt over all phase offsets is calculated as follows.

$$\overline{rtt} = \int_{0}^{1} rtt \, d\delta$$

=
$$\int_{0}^{1} \left\lceil dist + \delta \right\rceil + \left\lceil dist - \delta \right\rceil \, d\delta$$

=
$$2 \cdot dist + 1$$
 (3.5)

The variance of the quantization error is calculated as followed and is simplified to a cubic function of the fractional part of the round trip distance. Both the mean and variance are displayed in Figure 3.3.

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Figure 3.2: Round trip time versus distance and phase offsets



Figure 3.3: Theoretical mean distance and variance of distance.

$$\sigma^{2} = \int_{0}^{1} (\overline{rtt} - rtt)^{2} d\delta$$

= $\{2dist\} - \{2dist\}^{2}$
= $\frac{1}{4} - (\{2dist\} - \frac{1}{2})^{2}$ (3.6)

The rtt function produces a pattern repeating every phase period. This reoccurrence introduces a frequency component to be present in the observations. If two clocks interfere, their phases are equal every beat period (the reciprocal of the beat frequency). Thus, the impact of quantization errors causes a similar effect as the two interfering waves – namely a beat frequency.

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3.4 Limits and Verification

The accuracy of location and distance sensing algorithms have fundamental limits [22–26]. For example, the analytic calculations above do not take into account the clock drift during one RTT observation. Assuming a frequency stability of ± 25 ppm and a length of a transmission sequence of 60 μ s and 320 μ s, the maximal error could be up to 0.9 m and 4.8 m respectively.

Furthermore, one should note that only in vacuum light travels at the speed of light c. In materials the propagation speed depends on the square root of the dielectric constant ε . For example, dry ferroconcrete has an ε of about 9 and electromagnetic waves traverse through ferroconcrete 3 times slower than in vacuum. Most other materials used in buildings have lower dielectric constants.

Another source of possible errors is due to non-line-of-sight conditions. This results in an overestimation of the distance between the two nodes [27]. Multipath propagation might introduce measurement errors because the dominant path can vary depending on the current transmission conditions. Multipath propagation is present only if reflections are given. Reflections can have large impact on signal strength but only a low one on propagation delay. Thus, in the presence of multipath propagation or reflections, we assume time delay measurement as being more precise than those based on the RSSI.

In order to check these hypotheses and identify the real measurement resolution, we conducted experiments. The first measurement campaign was conducted to study the impact of slow-user motion on packet loss and delay as described in [18]. At the same time, we also measured the impact of distance on the round trip times. One year later, we embarked on a second measurement campaign. We altered the radio modem technology, the location, the analysis software, and the staff. Thus, we proved the reliability and correctness of our approach.

Measurements: First campaign

4.1 Experimental setup

The measurement was done in a gymnasium (Figure 4.1 and 7.6) [18]. The data communication takes place between the local and the remote node. ICMP ping packets were transmitted each 20 ms. The measurements of RTT were conducted for several distances (5, 10, 15, 20, 25, 30, 35, 40 m). At each distance, we measured for about 15 minutes. One should note that in this first campaign, the wireless LAN cards were close to the ground. Also, the directions of the antennas were selected at random and were not recorded. This is important to know, because it explains some of the results presented later.

4.2 Equipment

All PCs were running a Suse 6.4 Linux system with a 2.4.17 kernel. D-Link cards featuring an Intersil's (now Conexant) Prism2 chipset were employed as a wireless interface. Packets were directly sniffed on the MAC layer by the measurement tool 'Snuffle' [28].



Figure 4.1: First measurements: schematic experimental setup.

4.3 Configuration

WLAN networking technologies based on the IEEE 802.11 standards transmit data packets via air. Each data packet that is addressed to only one receiver is immediately acknowledged if it is received without errors. The receiver must send the acknowledgement instantaneously after data packet's arrival. Thus, the sender knows whether the transmission has been successful or whether it has to be redone. To avoid potential packet delay effects, in this experiments the maximal number of retransmissions (transmission type) was set to zero.

The data packet and the acknowledgement start with a preamble followed by a Physical Layer Convergence Procedure (PLCP) header which contains the length and modulation type. The length of the preamble and header are 144+48 μ s (802.11). After the PLCP header, the actually MAC frame body is sent immediately at the selected modulation type. In case of the data packets, the speed of the transmission (modulation type) was set to 11 Mbit/s. The MAC frame contains the header of MAC (24 b), IP (20 b), UDP (8 b), RTP (16 b), Voice (20 b) and the frame check sequence (4 b). Overall the MAC PDU has a length of 92 b, which takes 66.91 μ s to transmit. Thus, the overall length of the data packet is 258.91 μ s. The acknowledgement is shorter. The ACK frame has a length of only 10 b plus the CRC (4 b). At 2 Mbit/s it has a transmittion time of 192+56=248 μ s. Between the data packet and the acknowledgement the receiver waits of the Short Interframe Space (SIFS), which has a length of 10 μ s.

4.4 Time measurements

The WLAN card recorded the arrival time of packets at a resolution of 1 μ s without any variable latency. The precise point of time, at which the time stamp is recorded, is not documented. In case of the data packet, we assume that the arrival time is recorded at the start of the MAC packet. In case of the acknowledgement, it might be recorded after the MAC header. Thus, the local delay for the given configuration is about 66.91+10+192+56=324.91 μ s. This value closely fits the measured delay.

The Prism2 cards implement only the recording time stamps of incoming packets. But we needed both sending and receiving time stamps. Therefore, we decided to use a third PC to monitor the packets which the local node sends and receives. The monitor PC was placed close-by the sender to avoid any additional propagation delays that could falsify the measurements.

It will be straight forward to alter software and firmware of WLAN cards to record transmission time stamps, too. Due to legal constraints, we were not able to implement these changes by ourselves. We expect that WLAN chipset manufactures will provide firmware updates to support precise time stamps because they will benefit from customers using WLAN for location-aware services. Until then, we are required to use the third monitoring node.

4.5 Data collection & processing

Snuffle provides the packet traces of all 802.11 packets received at the monitoring node. We filteredout only the successful ping sequences which consist of an ICMP request, an acknowledgement, an ICMP response and again an acknowledgement (Figure 4.2). Other packets like erroneous transmissions, beacons, ARQ messages etc. are dropped. Due to hardware limitations of the WLAN card only a fraction of observations were recorded (Table 4.1).

# H	ostnane	chry	se ee tu-	berlin de						
# D	ate	Apr	16 2003			20				
# 1	ine	11:5	6:33 PM			20m				
# 1	ane	IFFE	802 11 RX	(prism2)						
# 1	D	v1		(),,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,						
# V	ersion	linu	x							
#ti	ne st	atus	nactine s	ilence signal	rate	rxflov	frame o	ontrol dur al	a2 a3 seg data	a len index
105	0530203	062591	1792	-1705691856	2 192	110 0	8 258	275783974877	275783975678	2353046519773
105	0530203	062874	1792	-1705691533	2 114	20 0	212 0	275783975678	163790373911495	136797026756687
105	0530203	064005	1792	-1705690438	2 117	110 0	8 258	275783975678	275783974877	2353046519773
105	0530203	064294	1792	-1705690114	2 192	20 0	212 0	275783974877	24297368239684	209314687168476
105	0530203	081979	1792	-1705672469	1 192	110 0	8 258	275783974877	275783975678	2353046519773
105	0530203	083111	1792	-1705671324	2 117	110 0	8 258	275783975678	275783974877	2353046519773
105	0530203	102088	1792	-1705652358	2 195	110 0	8 258	275783974877	275783975678	2353046519773
105	0530203	103077	1792	-1705651359	2 114	110 0	8 258	275783975678	275783974877	2353046519773
105	0530203	113402	1792	-1705641178	2 195	20 0	128 0	281474976710655	275783975678	2353046519773
105	0530203	121960	1792	-1705632473	1 192	110 0	8 258	275783974877	275783975678	2353046519773
105	0530203	122257	1792	-1705632150	1 111	20 0	212 0	275783975678	163789483900893	2353046519773
105	0530203	123482	1792	-1705630950	1 114	110 0	8 258	275783975678	275783974877	2353046519773
105	0530203	123780	1792	-1705630627	1 192	20 0	212 0	275783974877	24297536061405	2353046519773
105	0530203	142353	1792	-1705612081	1 192	110 0	8 258	275783974877	275783975678	2353046519773
105	0530203	143430	1792	-1705611012	2 111	110 0	8 258	275783975678	275783974877	2353046519773
105	0530203.	143724	1792	-1705510589	2 192	20 0	212 0	275783974877	24299663080278	2/2333605064/18
105	0530203	162097	1792	-1705592352	2 192	110 0	8 258	275783974877	275783975678	2353046519773
105	0530203	1633339	1792	-1705591102	2 111	110 0	8 258	2/5/839/56/8	2/5/839/48//	2353046519773
105	0530203	182212	1792	-1705572234	1 195	110 0	8 258	2/5/839/48//	2/5/839/56/8	2353046519773
105	0530203	103530	1792	-1705571109	1 100	20 0	0 250	2/5/037/50/0	2/5/037/40//	2353046517//3
1.0.5	11530/203	10.307.5	1792	1705570700	2 100	110 0	0 200	2/5/037/90//	2427/510334502	2202/12200021
	Remo	nte d	elav	-1705552177	2 107	20 0	212 0	275783975678	163792293370592	40479511724561
	Kenne		ciay	-1705551654	1 117	110 0	8 259	275703975670	275792974977	2252046519772
1.05	115 211 211 2	21576		-1705538831	2 117	20 0	128 0	201474976710655	275793974977	2353046519773
105	0530203	222069	1797	-1705532379	2 195	110 0	8 258	275783974877	275783975678	2353046519773
105	0530203	222420	1792	-1705532055	2 114	20 0	212 0	275783975678	163788878984676	198688229866103
105	0530203	223385	1792	-1705531065	2 117	110 0	8 258	275783975678	275783974877	2353046519773
105	0530203	223684		-1705530742	2 192	20 0	212 0	275783974877	24299143393242	69878201989569
				-1705512343	2 195	110 0	8 258	275783974877	275783975678	2353046519773
	Loca	al de	lav	-1705512019	2 114	20 0	212 0	275783975678	163789483900893	2353046519773

Figure 4.2: Snuffle trace file showing recorded data traffic (20 m measurement)

distance	trace file entries	,good' entries	corrupted entries	share of corrupted entries
5 m	14371	12722	1649	11.5%
10 m	21256	18450	2806	13.2%
15 m	89877	77440	12437	3.8%
20 m	10316	9344	972	9.4%
25 m	9864	8822	1042	10.6%
30 m	20095	18124	1971	9.8%
35 m	40776	35682	5094	12.5%
40 m	32750	29216	3534	10.8%

Table 4.1: Numbers of missing, invalid and valid observations.



Figure 4.3: Remote and local delay observations over time.

Only the delays fitting in the interval [323 μ s, 324 μ s] are considered in further calculations (Figure 4.3. Only a very few delay measurements were observed with the value of 322 and 325 μ s. These and all other delays were considered as measurement errors. Taken these packet sequences, the mean and variance of the remote delay and local delay were calculated. To check for stationary process properties, the autocorrelation function was calculated. The screening of data entries and the subsequent calculations were executed by a self-created C-program [29].

4.6 Results

The distance was directly derived from the measured propagation delay using equation (1.1). Assuming a Gaussian error distribution, we also plotted the confidence intervals in Figure 4.4 and Table 4.2. Usually, the calculated distances were always higher than the real distances. Also, in some measurements (e.g. 35 m) the air propagation time was significantly higher. Due to the experimental setup, we could not ensure that the direct line-of-sight path was taken. The remote node was placed directly on the ground. Thus, the Fresnel zone was violated and the direct transmission path was hampered. In radio communications, a Fresnel zone is a concentric ellipsoid, covering the radiation path. Fresnel zones result from diffraction by the circular aperture.

In Figure 4.5 the signal strength is displayed over the distance. Theoretically, the signal strength should decrease with distance. In this measurement campaign other factors, such as reflection, seem to be dominant. If one compares Figure 4.4 and Figure 4.5, it seems time measurements reflect the distance more precisely than RSSI but they have a higher variance and a larger confidence interval.

4.7 Analysis

In [29] we show that the measurements follow a weak stationary process, with a constant mean, variance and covariance (for a constant lag) (Figure 4.6). Thus, further statistical methods are applicable.



Figure 4.4: Distance as calculated from RTT versus actual distance between both nodes. 95% confidence levels are given.

actual	remote	local	one-way	calculated	standard
distance	delay	delay	delay	distance	deviation
[m]	[µs]	$[\mu s]$	[ns]	[m]	[m]
5	323.297	323.207	45.0	13.44	8.4400
10	323.359	323.205	77.0	23.12	13.1125
15	323.377	323.230	73.5	22.07	7.0690
20	323.396	323.238	79.0	23.74	3.7395
25	323.465	323.208	128.5	38.62	13.6165
30	323.450	323.216	117.0	35.11	5.1105
35	323.567	323.166	200.5	60.21	25.2050
40	323.481	323.192	144.5	43.31	3.3090

Table 4.2: Delays, calculated distance and deviation versus real distance.



Figure 4.5: Received signal strength indication versus distance. Confidence intervals are too small to be shown.



Figure 4.6: Mean and variance over time at 15 m. The mean varies by ± 36 ns resp. ± 18 ns around its average. The variance varies by ± 0.008 resp. ± 0.01 around its average.

Confidence intervals are meaningful only if the observations are independent. This assumption can be verified by the autocorrelation function. The time-lag dependent autocorrelation coefficients are presented as a graph in Figure 4.7. The 15 m and 40 m results are shown as an example. The graphs at other distances look similar. The autocorrelation for the local delay is low. It is smaller than ρ =0.05. Thus, the local delay measurements can be seen as independent. The autocorrelation of remote delay values has the form of a decaying cosinus wave. This kind of autocorrelation curve is found if the observations feature a constant frequency component. Indeed, this pattern manifests in the delay traces. The values of 323 and 324 occur block-wise in bursts. We also calculated an FFT over the packet delays. Assuming that each observation follows the previous after 20 ms, we identified a dominant frequency at about 3.5 Hz independent of the distance (Figure 4.8). However, the lower the packet error rate, the stronger this effect is.

We explain the effect displayed in Figure 4.7 with interference of both remote and local crystal clocks. Taken this explanation of quantization errors we can calculate the clock drift between both signals. Assuming a clocking of the MAC protocol at 1 MHz, the drift between both clocks is approximately $drift = \frac{f_{beat}}{f_1} = \frac{3.5Hz}{1MHz} = 3.5$ ppm. Usually, the tolerance of consumer grade quartz clocks is up to 25 ppm. Thus, we consider this explanation to be plausible.

Interestingly, the MAC processing is conducted in steps of 1 μ s. Thus, the MAC processing time is not precisely the SIFS interval but is rounded up to the next 1 μ s. However, the error is small so that receivers tolerate it.

In our quantization error analysis we calculated the variance which is up to¹/₄. A distance of one and a time unit of one in the analysis refer to 300 m or 1 μ s in the experiments. Then, the standard deviation would be 18.75 m or 62.5 ns at most. The standard deviation is between 3.3 and 25 m. Thus, the quantization error is not the only dominant effect and others such as thermal noise are important too.



Figure 4.7: Autocorrelation (=cross correlation of itself) is oscillating for remote delays – indicating a fundamental frequency component in observations.

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Figure 4.8: The fourier transformation of the observations shows a dominant frequency at 3.5 Hz, which is only present in the remote delays. Taken from the 40 m measurements.

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Measurements: Second Round

5.1 Experimental setup

The measurements were conducted outside in the countryside where one could expect the channel to be free of disturbing noise coming from other radiating devices. The measurements were extended to the maximal transmission range of 100 m. The sender was placed on a table, whereas the receiver was installed on top of a 1.5 m ladder. This was to guarantee that a large percentage of the Fresnel-zone, an elliptic space around the direct line-of-sight between both nodes is free of any obstacles harming the transmission. This time, the antennas were directed at each other. The schematic setup is displayed in Figure 5.1 and 7.7. A notebook acting as local node was sending out ICMP request packets. An access point was used as a remote node. Again, a monitoring PC close to the local node was required. Ping packets were sent every 10 ms until the monitor received up to 20.000 packets.

5.2 Equipment

We used an access point (Netgear FWAG114) supporting 802.11b/g and as remote node. The PCs were running under Linux, Suse 9.1, with a special 2.6 kernel. We used two different WLAN cards containing chip sets from Atheros and Conexant implementing IEEE 802.11 a,b and g. The Atheros cards (brand Netgear WAG-511, contained an AR5212 chip) are supported by the Madwifi device driver. We used the software version downloaded from the CVS server on the August 30^h , 2004. The Conexant cards (brand: Longshine LCS-8531G containing Prism-GT chipset with an ISL3890 as MAC-Controller) are controlled by the prism54.org device driver (date 28-06-2004, firmware 1.0.4.3.arm). During each measurement both the sender and monitor were equipped with cards of the same brand. We also altered the notebook to study the impact of the CPU speed: An Asus Centrino 1.5 GHz and an Amilo Celeron 850 MHz notebook were used. To gather the packet traces, we used tcpdump and libpcap instead of Snuffle.

5.3 Configuration

The measurements were conducted in seven different configurations to study the impact of the WLAN card, CPU clock and modulation type. We used the default configuration of WLAN cards and access point but changed the supported standard to 802.11g and set the modulation type to either 36 or



Figure 5.1: Setup of the second campaign

54 Mbit/s (Table 5.1 and 5.2). The frame length of the data packets are 65 bytes and of the acknowledgements 14 bytes.

In case of the IEEE 802.11g transmission mode, a packet starts with a preamble and PLCP header of 48+4 μ s. After the PLCP header, the MAC frame body is sent. Beside the MAC PDU is contains a minimum of 22 bits of the PLCP header and padding bits. The pad bit round up the data packet length because it can be only a multiple of 4 μ s. (An OFDM symbol has the length of 4 μ s.) In case of the OFDM modulation mode, the SIFS has a length of 16 μ s. All other values are similar to the 802.11b mode.

The transmission time for a data packet is 64 and 68 μ s respective the modulation rate of 54 and 36 Mbit/s. The length of the acknowledgement is 60, 56, 56 μ s for a transmission mode of 24, 36, and 56 Mbit/s.

5.4 Time measurements

The Atheros and Prism54 chipsets support time stamps of received packets with a resolution of 1 μ s similar to the Prism II chip set. Thus, again, a second notebook near the sender is required to measure both sending and receiving time stamp. Also, we modified the device drivers to record the received of a packet. After each interrupt, which is generated to notify the operating system about the received or transmitted packets, the current time stamps are saved. The time was measured with a libpcap time stamp. We also used a feature of Intel CPUs, which counts the CPU clock cycles. Linux supports reading the time stamp counter (TSC) with the rdtsc(...) function if the OS kernel has proper support included.

Mode	Chipset	Monitor	Request	Ack.	Responce	Ack.	
		CPU	$l \rightarrow r$	$r \rightarrow l$	$r \rightarrow l$	$l {\rightarrow} r$	
amilo_ath_36m	Atheros	850 MHz	54	24	36	24	
amilo_ath_54m	Atheros	850 MHz	54	24	54	24	
asus_ath 36m	Atheros	1.5 GHz	54	24	36	24	
asus_ath_54m	Atheros	1.5 GHz	54	24	54	24	l
asus_prism_36-54m	PrismGT	1.5 GHz	54	24	36	24	
asus_prism_36m	PrismGT	1.5 GHz	36	24	36	36	
asus_prism_54m	PrismGT	1.5 GHz	54	54	54	54	
	Mode amilo_ath_36m amilo_ath_54m asus_ath_36m asus_ath_54m asus_prism_36-54m asus_prism_36m asus_prism_54m	ModeChipsetamilo_ath_36mAtherosamilo_ath_54mAtherosasus_ath_36mAtherosasus_ath_54mAtherosasus_prism_36-54mPrismGTasus_prism_36mPrismGTasus_prism_54mPrismGT	ModeChipsetMonitor CPUamilo_ath_36mAtheros850 MHzamilo_ath_54mAtheros850 MHzasus_ath_36mAtheros1.5 GHzasus_ath_54mAtheros1.5 GHzasus_prism_36-54mPrismGT1.5 GHzasus_prism_36mPrismGT1.5 GHzasus_prism_36mPrismGT1.5 GHzasus_prism_36mPrismGT1.5 GHzasus_prism_54mPrismGT1.5 GHz	ModeChipsetMonitorRequest CPU $1 \rightarrow r$ amilo_ath_36mAtheros850 MHz54amilo_ath_54mAtheros850 MHz54asus_ath_36mAtheros1.5 GHz54asus_ath_54mAtheros1.5 GHz54asus_prism_36-54mPrismGT1.5 GHz54asus_prism_36mPrismGT1.5 GHz36asus_prism_54mPrismGT1.5 GHz36	ModeChipsetMonitorRequestAck. CPU amilo_ath_36mAtheros850 MHz 54 24amilo_ath_54mAtheros850 MHz5424asus_ath_36mAtheros1.5 GHz5424asus_ath_54mAtheros1.5 GHz5424asus_prism_36-54mPrismGT1.5 GHz5424asus_prism_36mPrismGT1.5 GHz5424asus_prism_36mPrismGT1.5 GHz5454asus_prism_54mPrismGT1.5 GHz5454	ModeChipsetMonitor CPURequestAck.Responce CPU $1 \rightarrow r$ $r \rightarrow l$ $r \rightarrow l$ $r \rightarrow l$ amilo_ath_36mAtheros850 MHz542436amilo_ath_54mAtheros850 MHz542454asus_ath 36mAtheros1.5 GHz542436asus_ath_54mAtheros1.5 GHz542454asus_ath_54mAtheros1.5 GHz542436asus_prism_36-54mPrismGT1.5 GHz362436asus_prism_36mPrismGT1.5 GHz362436asus_prism_54mPrismGT1.5 GHz545454	ModeChipsetMonitorRequestAck.ResponceAck. CPU $1 \rightarrow r$ $r \rightarrow l$ $r \rightarrow l$ $1 \rightarrow r$ $1 \rightarrow r$ amilo_ath_36mAtheros850 MHz54243624amilo_ath_54mAtheros850 MHz54245424asus_ath 36mAtheros1.5 GHz54243624asus_ath_54mAtheros1.5 GHz54243624asus_ath_54mAtheros1.5 GHz54243624asus_prism_36-54mPrismGT1.5 GHz36243636asus_prism_36mPrismGT1.5 GHz54545454

Table 5.1: Configuration: Modulation speed of MAC packets depending on direction and type.

Table 5.2: Configuration of the WLAN cards on a Linux system.

Sender configuration:	
> iwpriv ath0 eth0 mode 3	# 802.11g mode
> iwconfig ath0 rate 36M	# (or 54M) set a fix tx rate (Atheros)
> iwpriv eth0 rate 36M	# (or 54M) set a fix tx rate (Prism54)
> ping -i 0.01 -s 1 \$IPADDR	# send pings each 10 ms
Monitor configuration:	
> iwconfig ath0 eth0 mode monitor	# Monitormodus
> sysctl -w devath.ctlpkt=-2	# trace all headers (Atheros)
> iwpriv eth0 set_prismhdr 1	# trace all headers (Prism54)
> tcpdump -i ath0 eth0 -c 20000	
-n -e -s 231 -tt -w trace_filename	# trace 20000 packets including link layer header

5.5 Data collection & processing

Tcpdump recorded the packet trace and wrotes them to files. After the measurements we used an tcpdump to convert these files to plain text files (refer 7). Tcpdump had to been modified in order to print out the prism link-layer headers.

For statistical analysis the R project software turned out to be quite efficient. Thus, this time we applied R programs to calculate the data's analyse mean, variance and autocorrelation.

5.6 Results

Similar to the first campaign we calculated the distance from the time delay measurements. Figure 5.2 displays the remote (blue) and local delay (red) measurements, the number of overall observations (#) and the correlation coefficient (R) for the given configuration. A clear correlation between actual distance and calculated distance can be identified. In the middle graph, one can see that the larger the distance (and the worse the link quality), the larger the confidence interval becomes.

Figure 5.3 and 5.4 show the relation between distance and signal strength. The received signal strength (blue lines) decreases with distance. The correlation coefficient (R) is also given but one should consider that signal strength usually decays exponentially. Thus, the correlation coefficient should not be compared directly with Figure 5.2. Our measurement data also show, that the signal strength of received data packets and received acknowledgement packets are nearly the same regardless of the packet length.

We also calculated the distances with time measurements in the interrupt routine. We could not identify which time gathering method (jiffies or TSC) is better. There was a slightly better result using a faster CPU. However, measuring the propagation time with the interrupt routine seems to be far too imprecise.

5.7 Analysis

We also calculated the autocorrelation of local and remote delays (Figure 5.5, 7.8, 7.9 and 7.10). Interestingly, high and alternating correlation coefficients were only present, if we used the prism chipsets. With increasing distance and increasing error rate, the pattern vanishes. At farer distances the observations, which are based only on successful transmission, might follow each other not after exactly 20 ms but after a multiple of 20 ms. Thus, we can conclude that the effect is rather due to the elapsed time than to the number of successful transmissions.



Figure 5.2: Propagation delay (=calculated distance) vs. actual distance (plus 95% conf. intervals). (blue/upper lines=biased remote delay, red/lower lines=biased local delays). Each value is based on at least 1000 observations.



Figure 5.3: Atheros: Received signal strength indication (RSSI) vs. actual distance (plus 95% confidence intervals). Blue=remote packets' RSSI; red=local packets' RSSI; lines=data packets; dot-ted=acknowledgements



Figure 5.4: PrismGT: Received signal strength indication (RSSI) vs. actual distance (plus 95% confidence intervals). Blue=remote packets' RSSI; red=local packets' RSSI; lines=data packets; dot-ted=acknowledgements



Figure 5.5: Autocorrelation of local and remote delay. Between two observations a delay of at minimal 20 ms is present.

Conclusion

We have presented an algorithm on how to measure the air propagation time of IEEE 802.11 packets with a higher accuracy. Using two different experimental setups, we determined the precision of round trip time measurements. We use commercial WLAN cards, supporting IEEE 802.11b and 802.11g, implemented with three different WIFI chip sets. We have shown that such time measurements are possible even with off-the-shelf, commercial WLAN equipment and without additional signal processing.

To overcome the low resolution of the clocks, multiple observations have to be combined and smoothened. This can be done best during an ongoing data transmission at no additional cost. Otherwise, ICMP pings have to be sent for a few seconds to achieve a proper resolution.

The duration of distance determination is short enough to follow nodes moving at pedestrian speed. The tracking of faster nodes will require additional algorithms such as Kalman filters.

We explained why smoothing indeed helps to enhance the resolution of the time difference measurement so that distance measurements become possible. This effect can be due to the presence of measurement noise and to the beat frequency resulting from drifting clocks. To the best of our knowledge, especially the latter explanation is novel.

Our finding suggests that instead of RSSI the round trip time should be measured because it is correlated with the distance more strongly. In our gymnasium measurement the RSSI has not been useful to identify the distance because – due to reflections – the attenuation varied largely.

The contribution of this work is to show that neither synchronized, precise clocks nor special hardware is required if the propagation delay between two WLAN nodes is to be measured. This allows the implementation of easy-to-use, cheap and precise indoor positioning systems, which do not require maps containing signal strength distributions.

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Appendix

<pre># Hostname ch: # Date Ap) # Time 100 # Name IEE # ID v1 # Version Lir</pre>	ryse.ee.t r 17, 200 :36:35AM EE802.11 rux	u-berlin.de 13 RX (prism2)												
time	status	mactime	silence	signal	rate r	xflow	frame control	dur	al	a2	a3	seq da	ta_len i	index
10505686271095:	52 1792	-681940826	2	195	110 0		8	258	275783974877	275783975678	2352291545053	-27072 11.	-	-1
10505686271098	49 1792	-681940503	2	102	20 0		212	0	275783975678	163789487421497	64026088128063	16704 18	760 -	-1
10505686271105:	52 1792	-681939830	2	102	110 0		œ	258	275783975678	275783974877	2352291545053	-14464 11.	-	-1
10505686271108	46 1792	-681939507	2	192	20 0		212	0	275783974877	24297539582009	64026088128063	16704 18	760 -	-1
10505686271293	41 1792	-681921044	1	195	110 C		8	258	275783974877	275783975678	2352291545053	-27056 11.	-	-1
10505686271296.	32 1792	-681920721	1	102	20 0		212	0	275783975678	163789483900893	2352291545053	-19840 11.	51	-1
10505686271304	75 1792	-681919899	1	102	110 0		ω	258	275783975678	275783974877	2352291545053	-14448 11.	-	-1
10505686271307	75 1792	-681919576	1	192	20 0		212	0	275783974877	24297536062206	2352291545053	-32528 11.	sti	-1
10505686271493	03 1792	-681901081	2	192	110 C		8	258	275783974877	275783975678	2352291545053	-27040 11.	-	-1
10505686271495.	96 1792	-681900758	2	105	20 C		212	0	275783975678	163789483900893	2352291545053	-19824 11.	-	-1

Figure 7.2: Tracefile from the second experiment, modified tcpdump output for Atheros chipsets

		ap SNAP (0xaa), ssap SNAP (0xaa), cmd 0x03, IP 192.168.127.54 > .127.1: icmp 9: echo request seq 12129	edgment	ap SNAP (Oxaa), ssap SNAP (Oxaa), cmd OxO3, IP 192.168.127.1 > .127.54: icmp 9: echo reply sed 12129	edgment			dsap SNAP (0xaa), ssap SNAP (0xaa), cmd 0x03, IP 192.168.127.54 > 58.127.1: icmp 9: echo request seq 412	wledgment	dsap SNAP (0xaa), ssap SNAP (0xaa), cmd 0x03, IP 192.168.127.1 > 58.127.54: icmp 9: echo reply seq 412	wledgment			ap SNAP (0xaa), ssap SNAP (0xaa), cmd 0x03, IP 192.168.127.54 > .127.1: icmp 9: echo request seq 16671	adgment	ap SNAP (0xaa), ssap SNAP (0xaa), cmd 0x03, IP 192.168.127.1 > .127.54: icmp 9: echo reply seq 16671	edgment
		dsap SNAP (0xaa), ssap SNAP (0xaa), 168.127.1: icmp 9: echo request seq	lowledgment	dsap SNAP (Oxaa), ssap SNAP (Oxaa), 168.127.54: icmp 9: echo reply sed 1	iowledgment			<pre>C, dsap SNAP (0xaa), ssap SNAP (0xaa 2.168.127.1: icmp 9: echo request se</pre>	knowledgment	C, dsap SNAP (0xaa), ssap SNAP (0xaa 2.168,127.54: icmp 9: echo reply seq	knowledgment			dsap SNAP (0xaa), ssap SNAP (0xaa), 168.127.1: icmp 9: echo request seq	owledgment	dsap SNAP (Oxaa), ssap SNAP (Oxaa), 168.127.54: icmp 9: echo reply sed 1	owledgment
		00095B6625F4 0002DD441D22 LLC, 192.	0002DD441D22 0002DD441D22 Ackn	0002DD441D22 00095B6625F4 LLC, 192.	00095B6625F4 00095B6625F4 Ackn			00095B6625F4 0002DD441D22 LI	0002DD441D22 0002DD441D22 Ac	0002DD441D22 00095B6625F4 LI	00095B6625F4 00095B6625F4 Ac			00095B6625F4 0002DD441D22 LLC, 192.	0002DD441D22 0002DD441D22 Ackn	0002DD441D22 00095B6625F4 LLC,	00095B6625F4 00095B6625F4 Ackn
	oise Prea Enc FC Dur	90 0 0 0108 40	90 0 0 0004 0	90 0 0 0208 44	90 0 0 00D4 0		Noise Prea Enc FC D	190 0 0 0108 4	190 0 0 0004 0	190 0 0 0208 4	190 0 0 0004 4		oise Prea Enc FC Dur	22 0 0 0108 40	22 0 0 00D4 0	22 0 0 0208 44	22 0 0 00D4 4
)5m-p54-asus−1.dmp	n Rate Ant Prio SSI SIG 1	540 0 0 3 102 1	240 0 0 3 87 3	360 0 3 86	240 0 0 3 104	15m-p54-asus-1.dmp	Ch Rate Ant Prio SSI SI	6 360 0 0 3 83	6 240 0 0 3 57	6 360 0 0 3 56	6 360 0 0 3 83	15m-p54-asus-1.dmp	n Rate Ant Prio SSI SIG	540 0 0 3 102 3	240 0 0 3 85 2	540 0 0 3 77 2	540 0 0 3 102 2
6-INT54 np -tt -n -ee -r 54M-0.	Th Phy Ch	360 835360549772 6 6	124 835360627578 6 6	535 835362018440 6 6	572 835362101742 6 6	6-Int36 np -tt -n -ee -r 36M-0.	Th Phy	7765 2189271384862 6	7798 2189271467436 6	9832 2189272633530 6	3861 2189272711866 6	4-INT54 mp -tt -n -ee -r 54M-0.	Th Phy Ch	409 511113408117 6 6	472 511113486076 6 6	306 511114838416 6 6	951 511114922674 6 6
<pre>cd asus/prism_dump/ap36 tcpdump-3.8.3tkn/tcpdum</pre>	μL	108885589.199428 6166880	.088885589.199556 6166881	1088885589.201876 6166905	088885589.202014 6166905	<pre>> cd asus/prism_dump/ap36 > tcpdump-3.8.3tkn/tcpdum</pre>	шŢ	1088887824.044481 2851457	088887824.044568 2851457	1088887824.046512 2851459	.088887824.046642 2851459	<pre>> cd asus/prism_dump/ap54 > tcpdump-3.8.3tkn/tcpdum</pre>	Tm	1088890961.892849 1632374	088890961.892856 1632374	1088890961.892862 1632398	088890961.892869 1632398



			Con	figurat	ion: am	ilo_ath_5	4m				
Act.		Remo	ote dela	ays		Local delays					
dist.	mean	var	min	max	#	mean	var	min	max	#	
[m]	[µs]		[µs]	[µs]		[µs]		[µs]	$[\mu s]$		
5	39.531	0.249	39	40	4415	39.499	0.250	39	40	4681	
10	39.556	0.247	39	40	4306	39.492	0.250	39	40	4785	
15	39.579	0.244	39	40	4553	39.506	0.250	39	40	4721	
20	39.616	0.237	39	40	4553	39.512	0.250	39	40	4746	
25	39.655	0.226	39	40	4529	39.501	0.250	39	40	4683	
30	39.703	0.209	39	40	4073	39.496	0.250	39	40	4830	
35	39.719	0.202	39	40	4521	39.514	0.250	39	40	4585	
40	39.760	0.183	39	40	4437	39.512	0.250	39	40	4071	
45	39.790	0.166	39	40	3473	39.504	0.250	39	40	3727	
50	39.817	0.150	39	40	3962	39.502	0.250	39	40	3844	
55	39.875	0.109	39	40	3691	39.505	0.250	39	40	3794	
60	39.886	0.101	39	40	3969	39.507	0.250	39	40	4058	
65	39.920	0.074	39	40	2664	39.520	0.250	39	40	2873	
70	39.952	0.046	39	40	3429	39.553	0.248	39	40	311	
75	39.995	0.010	39	41	3237	39.511	0.250	39	40	3393	
80	40.017	0.018	39	41	3687	39.490	0.250	39	40	2900	
85	40.056	0.053	40	41	2741	39.497	0.250	39	40	3265	
90	40.086	0.079	40	41	2348	39.487	0.250	39	40	2456	
95	40.130	0.113	40	41	3688	39.429	0.247	39	40	98	
99	40.172	0.143	40	41	2857	39.500	0.258	39	40	32	
									-		
			Config	guratio	n: asus_	prism_36	-54m		-		
Act.		Remo	Config ote dela	guration ays	n: asus_	prism_36	-54m Loca	al delay	ys		
Act. dist.	mean	Remo var	Config ote dela min	guratio ays max	n: asus_ #	prism_36 mean	-54m Loca var	a l dela y min	y s max	#	
Act. dist. [m]	mean [µs]	Remo var	Config ote dela min [µs]	guratio ays max [μs]	n: asus_ #	prism_36 mean [µs]	-54m Loca var	al delay min [µs]	y s max [µs]	#	
Act. dist. [m] 5	mean [μs] 63.578	Remo var 0.244	Config ote dela min [µs] 63	guration ays max [µs] 64	n: asus_ # 4841	prism_36 mean [μs] 36.582	-54m Loca var 0.243	al delay min [µs] 36	$\max_{\substack{[\mu s]\\37}}$	#	
Act. dist. [m] 5 10	mean [μs] 63.578 63.668	Remo var 0.244 0.222	Config ote dela min [μs] 63 63	guration ays max [μs] 64 64	n: asus# 	prism_36 mean [μs] 36.582 36.569	-54m Loca var 0.243 0.249	al delay min [μs] 36 33	$max \\ [\mu s] \\ 37 \\ 38$	# 4850 4280	
Act. dist. [m] 5 10 15	mean [μs] 63.578 63.668 63.681	Remo var 0.244 0.222 0.217	Config Dte dela min [μs] 63 63 63 63	guration ays max [μs] 64 64 64	n: asus# 4841 4913 5101	prism_36 mean [μs] 36.582 36.569 36.563	-54m Loca var 0.243 0.249 0.250	al delay min [μs] 36 33 33	ys max [µs] 37 38 38	# 4850 4280 3790	
Act. dist. [m] 5 10 15 20	mean [µs] 63.578 63.668 63.681 63.740	Remo var 0.244 0.222 0.217 0.194	Config bte dela min [μs] 63 63 63 63 63	guration ays max [μs] 64 64 64 64 65	n: asus_ # 4841 4913 5101 5084	prism_36 mean [μs] 36.582 36.569 36.563 36.591	-54m Loca var 0.243 0.249 0.250 0.251	al delay min [μs] 36 33 33 32	ys [μs] 37 38 38 38 37	# 4850 4280 3790 2320	
Act. dist. [m] 5 10 15 20 25	mean [µs] 63.578 63.668 63.681 63.740 63.772	Remo var 0.244 0.222 0.217 0.194 0.177	Config bte dela min [μs] 63 63 63 63 63 63 63	guratio ays max [μs] 64 64 64 65 65	# 4841 4913 5101 5084 4836	prism_36 mean [μs] 36.582 36.569 36.563 36.591 36.591	-54m Loca var 0.243 0.249 0.250 0.251 0.242	hl delay min [μs] 36 33 33 32 36	ys max [μs] 37 38 38 37 38	# 4850 4280 3790 2320 4817	
Act. dist. [m] 5 10 15 20 25 30	mean [μs] 63.578 63.668 63.681 63.740 63.772 63.813	Remo var 0.244 0.222 0.217 0.194 0.177 0.153	Config bte dela min [μs] 63 63 63 63 63 63 63 63 63 63	guration hys max [μs] 64 64 64 64 65 65 65	n: asus # 4841 4913 5101 5084 4836 4740	prism_36 mean [μs] 36.582 36.569 36.563 36.591 36.591 36.563	-54m Loc: var 0.243 0.249 0.250 0.251 0.242 0.251	hl delay min [μs] 36 33 33 32 36 32	ys max [μs] 37 38 38 37 38 37 38 37	# 4850 4280 3790 2320 4817 4612	
Act. dist. [m] 5 10 15 20 25 30 35	mean [μs] 63.578 63.668 63.681 63.740 63.772 63.813 63.843	Remo var 0.244 0.222 0.217 0.194 0.177 0.153 0.134	Config bte dela min [μs] 63 63 63 63 63 63 63 63 63 63	guratio hys max [μs] 64 64 64 64 65 65 65 65 65	# 4841 4913 5101 5084 4836 4740 4884	prism_36 mean [μs] 36.582 36.569 36.563 36.591 36.563 36.563 36.561	-54m Loc: var 0.243 0.249 0.250 0.251 0.242 0.251 0.248	hl delay min [μs] 36 33 33 32 36 32 36 32 36	ys max [μs] 37 38 38 37 38 37 38 37 38	# 4850 4280 3790 2320 4817 4612 3022	
Act. dist. [m] 5 10 15 20 25 30 35 40	mean [μs] 63.578 63.668 63.681 63.740 63.772 63.813 63.843 63.843	Remo var 0.244 0.222 0.217 0.194 0.177 0.153 0.134 0.116	Config bte dela min [μs] 63 63 63 63 63 63 63 63 63 63 63 63 63	ys max [μs] 64 64 64 65 65 65 65 65 65	# 4841 4913 5101 5084 4836 4740 4884 3832	prism_36 mean [μs] 36.582 36.569 36.563 36.591 36.563 36.561 36.561 36.576	-54m Loca var 0.243 0.249 0.250 0.251 0.242 0.251 0.248 0.253	hl delay min [μs] 36 33 33 32 36 32 36 32	ys max [μs] 37 38 38 37 38 37 38 37 38 38	# 4850 4280 3790 2320 4817 4612 3022 3029	
Act. dist. [m] 5 10 15 20 25 30 35 40 45	mean [µs] 63.578 63.668 63.681 63.740 63.772 63.813 63.843 63.843 63.872 63.903	Remo var 0.244 0.222 0.217 0.194 0.177 0.153 0.134 0.116 0.090	Config bite dela min [μs] 63 63 63 63 63 63 63 63 63 63 63 63 63	ys max [μs] 64 64 64 65 65 65 65 65 65 65	# 4841 4913 5101 5084 4836 4740 4884 3832 3373	prism_36 mean [μs] 36.582 36.569 36.563 36.591 36.563 36.561 36.561 36.576 36.590	-54m Loca var 0.243 0.249 0.250 0.251 0.242 0.251 0.248 0.253 0.248	hl delay min [μs] 36 33 33 32 36 32 36 32 36 32 33	ys max [μs] 37 38 38 37 38 38 37 38 37 38 37 38 37 38 38 37 38 38 37 38 38 37 38 38 37 38 38 37 38 38 37 38 38 37 38 38 37 38 38 37 38 38 37 38	# 4850 4280 3790 2320 4817 4612 3022 3029 1887	
Act. dist. [m] 5 10 15 20 25 30 35 40 45 50	mean [μs] 63.578 63.668 63.681 63.740 63.772 63.813 63.843 63.843 63.872 63.903 63.953	Remo var 0.244 0.222 0.217 0.194 0.177 0.153 0.134 0.116 0.090 0.105	Config pie dela min [μs] 63	ys max [μs] 64 64 64 65 65 65 65 65 65 65 65	n: asus_ # 4841 4913 5101 5084 4836 4740 4884 3832 3373 899	prism_36 mean [μs] 36.582 36.569 36.563 36.591 36.563 36.561 36.576 36.576 36.590 36.615	-54m Loca var 0.243 0.249 0.250 0.251 0.242 0.251 0.248 0.253 0.248 0.241	hl delay min [μs] 36 33 33 32 36 32 36 32 33 36	ys [μs] 37 38 38 37 38 37 38 38 37 38 38 37 38 38 37 38 38 37 38 38 37 38 38 37 38 38 37 38 38 37 38 38 37 38 38 37 38 38 38 38 37 38 38 38 38 38 38 37 38 38 38 38 38 38 38 38 38 38	# 4850 4280 3790 2320 4817 4612 3022 3029 1887 509	
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Act. dist. [m] 5 10 15 20 25 30 25 30 35 40 45 50 55 60	$\begin{array}{c} \text{mean} \\ [\mu s] \\ \hline 63.578 \\ \hline 63.668 \\ \hline 63.681 \\ \hline 63.740 \\ \hline 63.772 \\ \hline 63.813 \\ \hline 63.843 \\ \hline 63.843 \\ \hline 63.872 \\ \hline 63.903 \\ \hline 63.903 \\ \hline 63.953 \\ \hline 64.012 \\ \hline 64.088 \end{array}$	Remo var 0.244 0.222 0.217 0.194 0.177 0.153 0.134 0.116 0.090 0.105 0.116 0.113	Config μ s] 63 63 63 63 63 63 63 63 63 63	$\begin{array}{c} \text{guration} \\ \text{nys} \\ max \\ [\mu s] \\ \hline 64 \\ 64 \\ 64 \\ 65 \\ 65 \\ 65 \\ 65 \\ 65 \\$	n: asus_ # 4841 4913 5101 5084 4836 4740 4884 3832 3373 899 577 1028	prism_36 mean [μs] 36.582 36.569 36.563 36.591 36.563 36.591 36.563 36.561 36.576 36.590 36.615 36.638 36.598	-54m Loca var 0.243 0.249 0.250 0.251 0.242 0.251 0.248 0.253 0.248 0.241 0.233 0.241	al delay min $[\mu s]$ 36 33 32 36 32 36 32 36 32 36 32 36 36 36 36 36 36	ys max [μs] 37 38	# 4850 4280 3790 2320 4817 4612 3022 3029 1887 509 149 408	
Act. dist. [m] 5 10 15 20 25 30 35 40 45 50 55 60 65	mean [μs] 63.578 63.668 63.681 63.740 63.772 63.813 63.843 63.872 63.903 63.953 64.012 64.088 64.109	Remo var 0.244 0.222 0.217 0.194 0.177 0.153 0.134 0.116 0.090 0.105 0.116 0.113 0.109	Config pte dela min [μs] 63 63 63 63 63 63 63 63 63 63 63 63 63	$\begin{array}{c} \text{guration} \\ \text{ays} \\ \text{max} \\ [\mu s] \\ \hline 64 \\ 64 \\ 64 \\ 65 \\ 65 \\ 65 \\ 65 \\ 65 \\$	n: asus_ # 4841 4913 5101 5084 4836 4740 4884 3832 3373 899 577 1028 3779	prism_36 mean [μs] 36.582 36.569 36.563 36.591 36.563 36.591 36.563 36.561 36.576 36.590 36.615 36.638 36.598 36.594	-54m Loca var 0.243 0.249 0.250 0.251 0.242 0.251 0.248 0.253 0.248 0.241 0.233 0.241 0.242	hl delay min [μs] 36 33 33 32 36 32 36 32 33 36 36 36 36 36 36	ys max [μs] 37 38 38 37 38 37 38 37 38 37 38 37 37 37 37	# 4850 4280 3790 2320 4817 4612 3022 3029 1887 509 149 408 505	
Act. dist. [m] 5 10 15 20 25 30 35 40 45 50 55 60 65 70	mean [μs] 63.578 63.668 63.681 63.740 63.772 63.813 63.843 63.843 63.872 63.903 63.953 64.012 64.088 64.109 64.107	Remo var 0.244 0.222 0.217 0.194 0.177 0.153 0.134 0.116 0.090 0.105 0.116 0.113 0.109 0.106	Config pite dela min [μs] 63	$\begin{array}{c} \text{guration} \\ \text{ays} \\ \text{max} \\ [\mu s] \\ \hline 64 \\ 64 \\ 64 \\ 65 \\ 65 \\ 65 \\ 65 \\ 65 \\$	# 4841 4913 5101 5084 4836 4740 4884 3832 3373 899 577 1028 3779 1558	prism_36 mean [μs] 36.582 36.569 36.563 36.591 36.591 36.591 36.563 36.561 36.576 36.590 36.615 36.638 36.598 36.594 36.557	-54m Loca var 0.243 0.249 0.250 0.251 0.242 0.251 0.248 0.253 0.248 0.241 0.233 0.241 0.242 0.241 0.242 0.247	al delay min $[\mu s]$ 36 33 33 32 36 32 36 32 33 36 36 36 36 36 36 36	ys max [μs] 37 38 38 37 38 37 38 37 38 37 38 37 37 37 37 37	# 4850 4280 3790 2320 4817 4612 3022 3029 1887 509 149 408 505 436	
Act. dist. [m] 5 10 15 20 25 30 35 40 45 50 55 60 65 70 75	mean [μs] 63.578 63.668 63.681 63.740 63.772 63.813 63.843 63.843 63.872 63.903 63.953 64.012 64.088 64.109 64.107 64.119	Remo var 0.244 0.222 0.217 0.194 0.177 0.153 0.134 0.116 0.090 0.105 0.116 0.113 0.109 0.106 0.105	Config interpretation of the delay min $[\mu s]$ 63 63 63 63 63 63 63 63 63 63	$\begin{array}{c} \text{guration} \\ \text{hys} \\ \text{max} \\ [\mu s] \\ \hline 64 \\ 64 \\ 64 \\ 65 \\ 65 \\ 65 \\ 65 \\ 65 \\$	# 4841 4913 5101 5084 4836 4740 4884 3832 3373 899 577 1028 3779 1558 513	prism_36 mean [μs] 36.582 36.569 36.563 36.591 36.563 36.561 36.576 36.590 36.615 36.638 36.598 36.594 36.557 36.588	-54m Loca var 0.243 0.249 0.250 0.251 0.242 0.251 0.248 0.253 0.248 0.241 0.233 0.241 0.242 0.241 0.242 0.247 0.244	al delay min $[\mu s]$ 36 33 33 32 36 32 36 32 33 36 36 36 36 36 36 36 36 36	ys max [μs] 37 38 38 37 38 37 38 37 38 37 38 37 37 37 37 37 37	# 4850 4280 3790 2320 4817 4612 3022 3029 1887 509 149 408 505 436 170	
Act. dist. [m] 5 10 15 20 25 30 35 40 45 50 55 60 65 70 75 80	$\begin{array}{c} \text{mean} \\ [\mu s] \\ \hline 63.578 \\ \hline 63.668 \\ \hline 63.681 \\ \hline 63.740 \\ \hline 63.772 \\ \hline 63.813 \\ \hline 63.843 \\ \hline 63.872 \\ \hline 63.903 \\ \hline 63.953 \\ \hline 64.012 \\ \hline 64.088 \\ \hline 64.109 \\ \hline 64.107 \\ \hline 64.145 \\ \end{array}$	Remo var 0.244 0.222 0.217 0.194 0.177 0.153 0.134 0.116 0.090 0.105 0.116 0.113 0.109 0.106 0.105 0.125	Config pie dela min $[\mu s]$ 63 64	$\begin{array}{c} \text{guration} \\ \text{ays} \\ \text{max} \\ [\mu s] \\ \hline 64 \\ 64 \\ 64 \\ 65 \\ 65 \\ 65 \\ 65 \\ 65 \\$	# 4841 4913 5101 5084 4836 4740 4884 3832 3373 899 577 1028 3779 1558 513 110	prism_36 mean [μs] 36.582 36.569 36.563 36.591 36.563 36.561 36.576 36.576 36.590 36.615 36.638 36.598 36.594 36.557 36.588 36.638	-54m Loca var 0.243 0.249 0.250 0.251 0.242 0.251 0.248 0.253 0.248 0.241 0.233 0.241 0.242 0.247 0.244 0.232	al delay min $[\mu s]$ 36 33 32 36 32 36 32 36 32 36 36 36 36 36 36 36 36 36 36 36 36 36	ys max [μs] 37 38 37 38 37 38 37 38 37 38 37 38 37 37 37 37 37 37 37 37	# 4850 4280 3790 2320 4817 4612 3022 3029 1887 509 149 408 505 436 170 152	
Act. dist. [m] 5 10 15 20 25 30 35 40 45 50 55 60 65 70 75 80 85	$\begin{array}{c} \text{mean} \\ [\mu s] \\ \hline 63.578 \\ \hline 63.668 \\ \hline 63.681 \\ \hline 63.740 \\ \hline 63.772 \\ \hline 63.813 \\ \hline 63.843 \\ \hline 63.843 \\ \hline 63.872 \\ \hline 63.903 \\ \hline 63.953 \\ \hline 64.012 \\ \hline 64.088 \\ \hline 64.109 \\ \hline 64.107 \\ \hline 64.119 \\ \hline 64.145 \\ \hline 64.203 \end{array}$	Remo var 0.244 0.222 0.217 0.194 0.177 0.153 0.134 0.116 0.090 0.105 0.116 0.113 0.109 0.106 0.105 0.125 0.163	Config pte dela min $[\mu s]$ 63 64 64	$\begin{array}{c} \text{guration} \\ \text{ays} \\ \text{max} \\ [\mu s] \\ \hline 64 \\ 64 \\ 64 \\ 64 \\ 65 \\ 65 \\ 65 \\ 65 \\$	n: asus_ # 4841 4913 5101 5084 4836 4740 4884 3832 3373 899 577 1028 3779 1558 513 110 133	prism_36 mean [μs] 36.582 36.569 36.563 36.591 36.563 36.561 36.576 36.590 36.615 36.598 36.594 36.557 36.588 36.588 36.638 36.638 36.600	-54m Loca var 0.243 0.249 0.250 0.251 0.242 0.251 0.248 0.243 0.248 0.241 0.233 0.241 0.242 0.247 0.244 0.232 0.300	al delay min $[\mu s]$ 36 33 32 36 32 36 32 36 36 36 36 36 36 36 36 36 36	ys [μs] 37 38 37 38 37 38 37 38 37 38 37 38 37 37 37 37 37 37 37 37 37	# 4850 4280 3790 2320 4817 4612 3029 1887 509 149 408 505 436 170 152 5	
Act. dist. [m] 5 10 15 20 25 30 35 40 45 50 55 60 65 70 75 80 85 90	$\begin{array}{c} \text{mean} \\ [\mu s] \\ \hline 63.578 \\ \hline 63.668 \\ \hline 63.681 \\ \hline 63.740 \\ \hline 63.772 \\ \hline 63.813 \\ \hline 63.843 \\ \hline 63.843 \\ \hline 63.843 \\ \hline 63.872 \\ \hline 63.903 \\ \hline 63.953 \\ \hline 64.012 \\ \hline 64.088 \\ \hline 64.107 \\ \hline 64.107 \\ \hline 64.107 \\ \hline 64.145 \\ \hline 64.203 \\ \hline 64.222 \end{array}$	Remo var 0.244 0.222 0.217 0.194 0.177 0.153 0.134 0.116 0.090 0.105 0.116 0.105 0.105 0.105 0.125 0.163 0.173	Config ote dela min $[\mu s]$ 63 64 64	$\begin{array}{c} \text{guration} \\ \text{max} \\ [\mu s] \\ \hline 64 \\ 64 \\ 64 \\ 64 \\ 65 \\ 65 \\ 65 \\ 65 \\$	# 4841 4913 5101 5084 4836 4740 4884 3832 3373 899 577 1028 3779 1558 513 110 133 1418	prism_36 mean [μs] 36.582 36.569 36.563 36.591 36.563 36.561 36.576 36.590 36.515 36.598 36.594 36.557 36.588 36.638 36.638 36.600 36.639	-54m Loca var 0.243 0.249 0.250 0.251 0.242 0.251 0.248 0.253 0.248 0.241 0.233 0.241 0.242 0.241 0.242 0.247 0.244 0.232 0.244 0.232 0.300 0.237	al delay min $[\mu s]$ 36 33 32 36 32 36 32 36 36 36 36 36 36 36 36 36 36	ys max [μs] 37 38 37 38 37 38 37 38 37 38 37 38 37 37 37 37 37 37 37 37 37 37	# 4850 4280 3790 2320 4817 4612 3022 3029 1887 509 149 408 505 436 170 152 5 36	

Table 7.1: Second Campaign: Distance vs. round trip time

			Conf	igurati	on: asu	s_prism_3	56m			
Act.		Remo	ote dela	ays		Local delays				
dist.	mean	var	min	max	#	mean	var	min	max	#
[m]	[µs]		[µs]	$[\mu s]$		[µs]		[µs]	$[\mu s]$	
5	32.215	0.170	31	33	4871	28.556	0.250	25	30	4826
10	32.283	0.203	32	33	4787	28.565	0.249	25	29	4410
15	32.282	0.202	32	33	4891	28.578	0.245	28	30	3979
20	32.302	0.211	31	33	4956	28.564	0.246	27	29	4479
25	32.318	0.217	32	33	4965	28.561	0.247	28	30	4429
30	32.351	0.228	32	33	4411	28.590	0.247	25	29	2524
35	32.378	0.235	32	33	4678	28.521	0.250	28	29	3275
40	32.415	0.243	32	33	4802	28.561	0.248	28	30	4132
45	32.438	0.246	32	33	3439	28.552	0.247	28	29	1689
50	32.463	0.249	32	33	2953	28.586	0.243	28	29	1461
55	32.506	0.250	32	34	4490	28.565	0.246	28	29	490
60	32.533	0.250	32	34	3079	28.551	0.250	28	30	881
65	32.590	0.242	32	33	3052	28.560	0.256	25	29	1298
70	32.619	0.236	32	33	2799	28.524	0.250	28	29	550
75	32.666	0.223	32	34	2236	28.581	0.244	28	29	246
			Conf	ìgurati	on: asu	s_prism_5	54m			
Act.	t. Remote delays						Loca	al delay	7S	
dist.	mean	var	min	max	#	mean	var	min	max	#
[m]	[µs]		[µs]	$[\mu s]$		[µs]		[µs]	$[\mu s]$	
Act.		Remo	ote dela	iys			Loca	al delay	y S	
dist.	mean	var	min	max	#	mean	var	min	max	#
[m]	$[\mu s]$		[µs]	$[\mu s]$		[µs]		[µs]	$[\mu s]$	
5	63.602	0.240	63	64	4681	44.622	0.240	44	49	4552
10	63.672	0.221	63	64	4730	44.619	0.237	44	46	3551
15	63.702	0.210	63	65	4588	44.607	0.240	44	46	4448
20	63.732	0.197	63	65	4716	44.602	0.241	44	46	4158
25	63.791	0.166	63	65	4549	44.600	0.241	44	46	4354
30	63.833	0.140	63	65	5051	44.625	0.240	44	48	3472
35	63.849	0.130	63	65	5634	44.619	0.238	44	46	1784
40	63.866	0.118	63	65	4412	44.618	0.238	44	46	1465
45	63.899	0.101	63	65	4556	44.629	0.237	44	46	625
50	63.931	0.100	63	65	2448	44.650	0.229	44	45	180
55	64.068	0.113	63	65	6805	44.333	0.333	44	45	3
60	64.073	0.109	63	65	1516	NA	NA	NA	NA	0
65	64.092	0.108	63	65	4264	44.650	0.229	44	45	120
70	64.131	0.122	63	65	1254	NA	NA	NA	NA	0
75	64 127	0.118	63	65	1824	NA	NA	NA	NA	0
	01.127	0.110				1				



Figure 7.4: Distance vs. delay using libpcap time stamps.



Figure 7.5: Distance vs. delay using the CPU's time stamp counter (TSC)



(a) Local node and monitor



(b) Direct line of sight

(c) Notebook at 30m





(a) Local and monitor node

(b) Remote node

Figure 7.7: Photos from the second campaign



Figure 7.8: Autocorrelation of local and remote delay. Between two observations a delay of at minimal 20 ms is present. Distance is 5 m.



Figure 7.9: Autocorrelation of local and remote delay. Between two observations a delay of at minimal 20 ms is present. Distance is 25 m.



Figure 7.10: Autocorrelation of local and remote delay. Between two observations a delay of at minimal 20 ms is present. Distance is 60 m.

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