

Dynamic routing at different layers in IP-over-WDM networks – Maximizing energy savings[☆]

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Abstract

We estimate potential energy savings in IP-over-WDM networks achieved by switching off router line cards in low-demand hours. We compare three approaches to react on dynamics in the IP traffic over time, FUFL, DUFL and DUDL. They provide different levels of freedom in adjusting the routing of lightpaths in the WDM layer and the routing of demands in the IP layer. Using MILP models based on three realistic network topologies as well as realistic demands, power, and cost values, we show that already a simple monitoring of the lightpath utilization in order to deactivate empty line cards (FUFL) may bring substantial benefits. The most significant savings, however, are achieved by rerouting traffic in the IP layer (DUFL). A sophisticated reoptimization of the virtual topology and the routing in the optical and electrical domains for every demand scenario (DUDL) yields nearly no additional profits in the considered networks. These results are independent of the ratio between the traffic demands and capacity granularity, the time scale, distribution of demands, and the network topology for DUFL and DUDL. The success of FUFL, however, depends on the spatial distribution of the traffic as well as on the ratio of traffic demands and lightpath capacity.

Keywords: network design, energy efficiency, power consumption, multi-layer, multi-hour, multi-period

1. Introduction

In the light of scarce resources and the rising demand for energy there is a growing interest in solutions and “green” strategies in different fields to reduce the power consumption [2]. In this work, we focus on energy-efficiency in IP (Internet Protocol) over WDM (Wavelength Division Multiplexing) backbone networks.

Telecommunication networks are typically dimensioned to handle an estimated worst-case traffic scenario. The classical approach to network design hence assumes a given single traffic matrix; see [3, 4, 5, 6, 7] and the references therein. This matrix can be estimated, e.g., by using population statistics [8] or by exploiting information from current traffic measurements [9]. To handle future changes in the traffic volume and potential peaks in high-demand hours, the demand values are very often (highly) overestimated. This conservative approach leads to static solutions supporting

all potential traffic patterns, but results in overprovisioned networks and a waste of CAPEX (capital expenditures) as well as OPEX (operational expenditures). Several attempts have been made to handle traffic uncertainty already in the design process stemming from stochastic or robust optimization [10, 11, 12, 13].

This work rather focuses on traffic engineering, given a statically designed, capacitated multi-layer network. Our aim is to dynamically adapt the routing and the number of active components to the traffic patterns reducing OPEX, where energy is one of the key factors. Nowadays the power consumption of IP routers and line cards is almost independent of the load and may reach thousands of kilowatts in total [14, 15, 16]. We pose the question of how much energy can be potentially saved by dynamically switching off idle IP router line cards in low-demand hours. Starting from a static base network, we compare three different approaches to make line cards idle by reconfiguring the routing at the IP and/or WDM layer. These approaches correspond to three different levels of freedom to dy-

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ynamically change the routing in the WDM and IP layers. They are presented in Section 2 together with the used network model.

Although several papers have focused on power consumption in single- and multi-layer networks (see Section 3), our work is, to the best of our knowledge, the first study comparing the contribution of rerouting at different layers to the energy savings. Using realistic data on dynamic traffic, network topologies, costs, and power of single network elements, we systematically investigate the influence of traffic variability on power consumption of dynamically reconfigurable networks. As shown in Section 4, we use variations of the same mixed integer linear program (MILP) to design a static base network, and to reconfigure the network in every demand scenario such as to maximize the number of idle line cards. This approach allows us to provide provable energy optimal solutions or at least upper bounds on the potential savings. Section 5 describes the used data. The computational study in Section 6 reveals that allowing dynamic routing at the IP layer depending on the traffic pattern contributes the most to the energy savings. Reconfiguring lightpaths in the WDM layer gives only little additional benefit. Section 7 concludes our work.

2. Network model

We focus on IP-over-WDM networks, where the WDM layer offers optical bypass technology, as depicted in Fig. 1 (a). Nodes in the WDM layer, which represent optical cross-connects (OXCs), are interconnected by links representing optical fibers. Each fiber carries up to B WDM channels of capacity C Gbps each. OXCs may connect incoming WDM channels to outgoing ones, or terminate them in the corresponding nodes in the IP layer. The IP layer is interconnected with the WDM layer by colored router line cards (see Fig. 1(b)), which provide a direct interface between IP and WDM by performing optical-electrical-optical (OEO) conversion. IP routers can be equipped with line cards of capacity C Gbps. Lightpaths, which are concatenations of WDM channels, terminate in the line cards. All parallel lightpaths between two IP routers form a virtual link (of capacity corresponding to the number of lightpaths between these routers) in the IP layer. The virtual links together with the IP routers form a virtual topology. All IP routers are sources and destinations of aggregated backbone traffic, which is converted into an optical signal by the line cards and directly fed into OXCs.

We assume full wavelength conversion capability, and leave the wavelength assignment and installation of converters to a postprocessing step [17].

Lightpaths between the same two IP routers may be established using different physical paths. Similarly, we assume that IP traffic can be arbitrarily split and routed via multiple virtual paths which is enabled for instance by traffic engineering techniques such as Multi-protocol Label Switching (MPLS). Notice that the main motivation behind the latter assumption is computational tractability; see Section 4. However, the energy saving approaches presented below are not restricted to any kind of IP routing.

A (CAPEX) cost-minimized static multi-layer network serves as a starting point to our investigations. Given demands with temporal and spatial dynamics, it is designed to accommodate all traffic without changing the routing and hardware configuration. Based on this static base network, we consider three different approaches to decrease power consumption in the operational phase by switching off unused line cards.

Fixed Upper Fixed Lower (FUFL): Both the routing of IP traffic in the upper virtual layer and the realization of lightpaths in the lower WDM layer are fixed over time. Demands are routed as in the static base network, using the same lightpaths with the same percental splitting as in the base network. We allow to shift traffic between parallel lightpaths though. Line cards of empty lightpaths are switched off.

Dynamic Upper Fixed Lower (DUFL): The virtual topology (including the realization of lightpaths) is fixed as in FUFL (Fixed Lower), but the routing of IP traffic can be changed (Dynamic Upper). In every demand scenario, we aim at routing the IP demands in the virtual topology in such a way that as many lightpaths as possible are emptied in order to switch off the corresponding line cards.

Dynamic Upper Dynamic Lower (DUDL): Both the routing of the IP traffic in the virtual layer and the realization of lightpaths in the physical layer can be changed over time, with the restriction that the number of installed line cards at each IP router must not be exceeded. The number of used line cards is minimized by jointly optimizing the routing in the IP and WDM layers.

A Fixed Upper Dynamic Lower approach is not feasible, since the IP routing has to react to changes of the virtual topology. Note that the terms Fixed Lower and Dynamic Lower apply to dynamics of the realization of the virtual topology. Idle light-

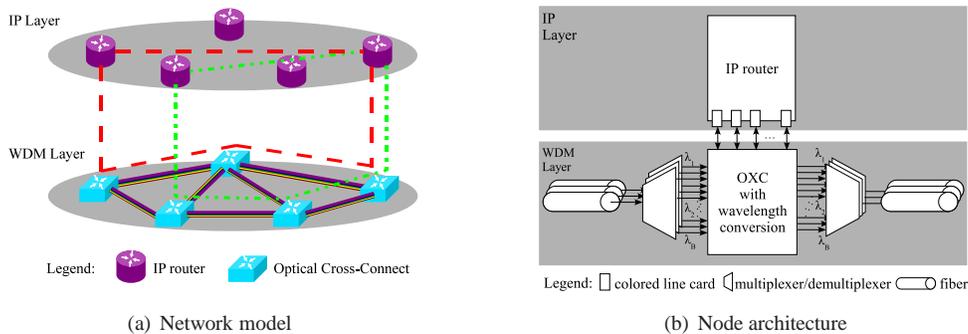


Figure 1: IP-over-WDM network: optical cross-connects interconnected by fibers constitute the physical topology, and IP routers interconnected by lightpaths constitute the virtual topology

paths are dynamically switched off in all the considered approaches.

Fig. 2 shows a simple example illustrating how the approaches FUFL, DUFL and DUDL can decrease the number of active line cards in a low-demand hour. We limit the number of nodes, links and demands in this example in order to keep it clear and easy to follow. The physical fiber installation and the hardware configurations at the nodes from the base network are fixed for all approaches. New line cards must not be installed. Two traffic matrices are considered. The static base network is designed to accommodate the peak traffic matrix. The approaches FUFL, DUFL and DUDL are applied in the low-demand hour starting from the base network. The columns of the subfigures in Fig. 2 correspond to the base network, FUFL, DUFL and DUDL respectively. The first row shows the routing of the IP demands, the second one depicts the virtual topologies, and the last one illustrates the routing of lightpaths over the physical topology. FUFL can switch off a lightpath between nodes *A* and *C* (the dotted one routed via *D* in Fig. 2(i)) due to a decrease of traffic. DUFL changes the routing of IP demands to additionally make the lightpaths *AC* (dotted, routed via *B* in Fig. 2(ii)) and *CD* idle. Eventually, DUDL adds a virtual link between nodes *B* and *C*, which does not exist in the base network (compare Fig. 2(e) and (h)). This additional link and the new routing of the IP demands allows to further decrease the number of active line cards.

FUFL is the most restrictive option. It is the easiest to be realized in practice since it does not require any optimization but only monitoring of the lightpath utilization. Decisions on switching line cards on and off can be taken locally. Its drawback is to rely on the routing defined by the base network, no matter what it is (single-path, weighted multi-path, etc.). The routing taken from the static

base network can be suboptimal especially in low-demand hours.

In contrast, DUFL and DUDL with the objective of minimizing number of lightpaths are NP-hard optimization problems, as they generalize the uncapacitated fixed charge flow problem [18, 19]. DUFL is a single-layer network design problem which can be solved to optimality in a reasonable amount of time in practice; see Section 6 and [4, 5]. DUDL is a computational challenge since it involves optimizing two coupled network layers simultaneously, similar to designing the base network; see [7, 20, 21, 22, 23].

Dynamics in the IP routing (DUFL) may allow more line cards to be switched off, compared to FUFL, by choosing a smart IP routing in each demand scenario, but it may lead to instabilities of connection-oriented protocols (e.g. due to overtaking of packets upon the change of the IP routing). Moreover, decisions about the IP routing changes need to be forwarded to all involved routers. Even more signaling is needed for additional dynamics in the WDM layer (DUDL). It has to be ensured that no packets are lost in the reconfiguration phase, when lightpaths are torn down. (G)MPLS including the traffic engineering extensions is a potential candidate for controlling and managing the paths. The reconfiguration itself is non-trivial though since it requires the use of OXCs to dynamically change virtual links (typically realized by point-to-point connections nowadays). Energy-efficient network design may have an influence on resilience and QoS (Quality of Service) in the network in terms of packet delay, jitter, packet loss as well as on network throughput, since switching off line cards decreases the capacity of the network. Moreover, network devices being repeatedly switched on and off may be more prone to failures.

The detailed study of such operational issues as

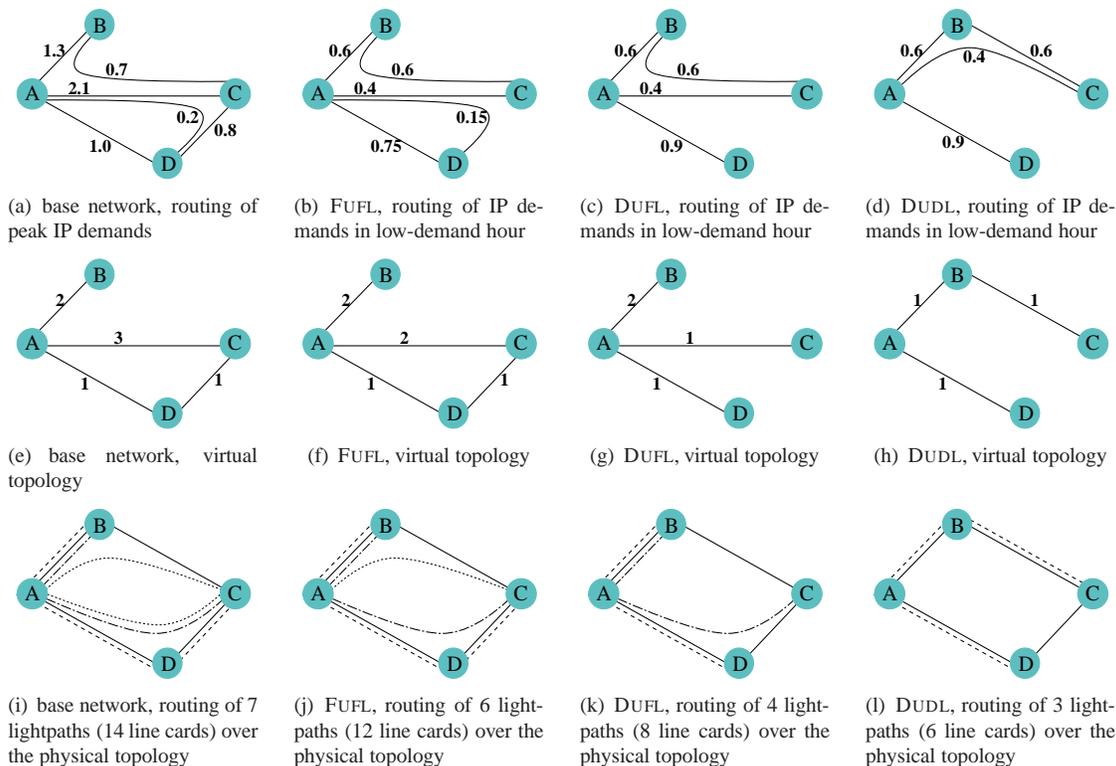


Figure 2: A simple example showing how the approaches FUFL, DUFL and DUDL decrease the number of active line cards. There are five peak demands ($AB = 1.3$, $AC = 2.1$, $AD = 1.2$, $BC = 0.7$, $CD = 0.8$), which decrease in the low-demand hour ($AB = 0.6$, $AC = 0.4$, $AD = 0.9$, $BC = 0.6$, $CD = 0.0$). The physical topology is fixed (solid lines in subfigures (i)–(l), each line corresponds to a single fiber of capacity $B = 3$ wavelengths). The granularity of the virtual link capacity is $C = 1$ (two line cards). In the low-demand hour 2, 6, and 8 line cards are saved with FUFL, DUFL, and DUDL, respectively.

mentioned above is beyond the scope of this paper. We also do not provide an algorithm or protocol to actually reconfigure the network when the traffic demand changes. Indeed, the goal of this paper is to compare the three approaches from a conceptual perspective and to give an upper bound on their energy saving potential. In this respect, the savings with DUDL serve as an upper bound for those with DUFL, which in turn serves as a benchmark for the more restrictive FUFL. In practice, a trade-off between potential energy savings and the complexity of reconfiguration needs to be found on a given time scale.

3. Related work

Although energy saving is quite a new subject in the wireline networking research, it has already been addressed in numerous papers since the pioneering work by Gupta and Singh [16]. We focus on routing to save energy and divide the papers into three groups depending on the dynamics of routing at different network layers. We look at the source

of the saving potential (what kind of network elements can be switched off), the approach taken to determine the energy savings (analytical, optimization or simulation), the considered scenarios (topology, traffic, power and cost values) and the dynamics of the network over time.

Dynamic routing in the optical layer: The Power-Aware Routing and Wavelength Assignment (PA-RWA) problem is proposed by Wu et al. [24] and formulated as a MILP. Energy savings can be achieved by switching off OXCs and optical amplifiers according to three proposed algorithms. A rough lower bound is also presented. Investigations of bidirectional rings and generic meshes of up to 32 nodes without wavelength conversion, and with a large number of fibers on each link and of wavelengths per fiber compared to the number of lightpaths (random requests with no dependency on time) revealed that smart routing of lightpaths in the WDM layer may bring significant energy savings against the shortest path routing and first fit wavelength assignment. The authors assume that both the power of an amplifier and the power of an

OXC are equal to 1 kW, however no justification for this value is given.

Silvestri et al. [25] make use of traffic grooming and transmission optimization to reduce energy consumption in the WDM layer. Traffic grooming shifts traffic from some fiber links to other ones in order to switch empty ones off, and transmission optimization adjusts dispersion management and pulse duration which decreases the need for using in-line 3R regenerators. Taking the simulative approach (OPNET SP Guru Transport Planner), the authors consider a European transport network (26 nodes and 46 links) with and without OXCs, and scale a traffic matrix to mimic changing demands. The power consumption of an optical amplifier is estimated to 200-500 W and the power of a 3R regenerator to 2-5 kW (unreferenced). The results show that transmission optimization may lead to the elimination of in-line 3R regenerators, and that traffic grooming allows to switch off significant number of links.

B. G. Bathula and M. Alresheedi and J. M. H Elmighani [26] leverage node clustering and any-cast routing to obtain a trade-off between the energy consumption and the average requests lost due to the sleep cycles of nodes in the clusters. In order to allow clusters to be switched to an OFF state, requests are destined to a set of nodes. If a destination cannot be reached due to its intermediate node belonging to a cluster in an OFF state, the next available destination can be chosen under acceptable bit-error-rate (BER) and propagation delay. The proposed algorithm is applied to the NSF network (14 nodes and 21 links) with four clusters, where call arrivals follow a Poisson process. Total power is calculated using the energy per bit for a core wavelength routing node (WRN) and for an optical amplifier (approximately 10 nJ and 0.1 nJ respectively) as well as the power of a transmitter and a receiver (unreferenced). The authors discuss the simulation results in the light of a trade-off between the average power consumed for each request and average request blocking as functions of load in Erlangs and number of clusters in an OFF state.

Dynamic routing in the electrical layer: Electrical network components offer a high potential of energy savings due to their high power consumption [27, 28, 29]. Usage of dynamic routing in the electrical layer for energy saving has been investigated in several papers. Many of the approaches presented there share the concept with DUFL.

Chabarek et al. [15] introduce power-aware network design, where power consumption is reduced

by adjusting routing of flows, choosing appropriate chassis type at each node in terms of capacity and power, and allocating appropriate number and type of line cards at each chassis. The proposed MILP minimizes power of all the chassis and line cards in the network. The authors support their approach with measurements of power consumption of routers (Cisco GSR 12008 and Cisco 7507). They point out that the power consumed by the routers shows only little dependency on the load (data rate, packet size, packet inter-arrival times). Despite router chassis being the most power-hungry elements of the router, its power consumption is highly dependent on the number and type of installed line cards. Using the power measurements and the MILP the authors investigate power consumption of 3 random and 4 Rocketfuel networks (7-21 nodes, 18-134 links) with traffic matrices generated according to the gravity model. The traffic is scaled with several factors in order to observe changes of power consumption in dependence of the load. The dynamics of traffic over time is not considered. After relaxing some constraints, the authors find out that minimum power consumption coincides with chassis that can accommodate a large number of line cards and line card capacities that closely match demand.

Chiaraviglio et al. [30, 31] focus on power consumption in hierarchical networks, where it is possible to turn off nodes and links. They consider a single-layer routing problem with time-varying demands, model it with a MILP [30], and use numerous heuristics [30, 31] to solve it. Randomly generated network topologies consisting of 10 core nodes, 30 edge nodes and 120 aggregation nodes are considered in [30], and a network similar to the one of the largest Internet Service Providers (ISPs) in Italy consisting of 8 core nodes, 52 backbone nodes, 52 metro nodes and 260 feeders is considered in [31]. A matrix of traffic demands between the aggregation nodes [30] and feeders [31] is randomly generated. In order to mimic the dynamics of traffic over time, the traffic matrix is scaled by a sinusoidal [30, 31] and the ISP's profile [31]. Time intervals of 5 minutes over a day are considered. The authors show significant reduction of power consumption with the proposed heuristics. While [30] reports on the percentages of nodes and links that can be switched off, [31] assumes unreferenced power values of amplifiers and router interfaces.

Multiple physical cables forming bundled links are considered in [32]. Authors propose three heuristics to maximize shutdown cables, and in-

investigate three network topologies (a hierarchical one with 50 nodes and 148 links, Waxman with 50 nodes and 169 links, and Abilene with 39 nodes and 28 links) under traffic demands generated with a classical entropy model. Reported relative energy savings versus bundle size (number of cables in a logical link) reveal that the energy savings increase sharply as the bundle size increase to 2 or 3, and that the performances of the three heuristics are almost indistinguishable. Authors discuss also the running time of the heuristics, which range from 6 seconds to 7 minutes for the Abilene network. Performance of the heuristics under dynamic traffic is not discussed.

Energy Profile Aware Routing (EPAR) introduced by Restrepo et al. [33] assumes the dependency between the energy consumption and the traffic load or traffic throughput of a particular network component, which is referred to as the Energy Profile. Energy can be saved by choosing components with appropriate Energy Profiles. EPAR (formulated as a linear equation system) using five Energy Profiles for routers (energy consumption range 0 - 15 kWh under 0 - 3.2 Tbps traffic, respectively) is evaluated on a Germany50 network (50 nodes, 88 links) under fully-meshed traffic (no further details about the traffic available, traffic dynamics not considered). Shortest (least hop) path routing is used as a reference. Significant energy savings are shown. Cubic Energy Profiles turn out to be especially efficient. Convex profiles achieve higher energy savings (against the shortest path routing) than the concave ones due to multi-path routing making use of low power consumption over broader load range.

Energy-Aware Traffic Engineering (EATe) introduced by Vasić and Kostić [34] is another approach for energy saving. Changing routes aims not only at switching off links and routers, but also at rate adaptation. The authors evaluate EATe on five Rocketfuel topologies (19-115 nodes, 68-296 links) using ns-2 simulations, TRUMP traffic and given drop margin, which determines the number of links that EATe tries to push to a lower energy level. Four uniformly distributed energy operating rates with quadratic energy savings between them are used, and relative energy savings are reported. It is shown that EATe manages to completely remove traffic on up to 31% of the links (depending on the number of alternative paths for the traffic in the network), without a significant increase of link utilizations. It is also possible to put routers to sleep with little increase of link utilizations, as well as make use of rate adaptation. Based on link

utilizations the authors predict that most of the time EATe will have negligible impact on latency. Stability of EATe under traffic changes and handling of link failures are also presented.

Puype et al. [35, 36] investigate multi-layer traffic engineering with the objective of reducing the power consumption in IP-over-optical networks. They assign higher routing costs to lightly loaded logical links in order to empty them after IP rerouting. Empty logical links are removed from the actual logical topology to save energy. Since routing of logical links is not considered, we classify this work as dynamic routing in the electrical layer. Applying an algorithmic approach to a 14-node network under a traffic pattern based on a uniform distribution, the authors show significant power savings against a full-mesh logical topology. Traffic characteristics cover diurnal traffic variations - off-hour traffic is equal to 0.25 of the peak traffic. Authors investigate the case when logical topology updates are slower than the diurnal traffic variations and the opposite one under the assumption that power of router interfaces (line cards) depends on the carried traffic. The authors discuss two ways to influence the power versus bandwidth (load) curve, i.e. idle power reduction (by e.g. matching line rates with traffic volume, or reducing clock rates) and the scaling of equipment power requirements using newer CMOS technology. Both of them influence the results of the considered traffic engineering approach. Normalized power values against the maximum power are reported.

Dynamic multi-layer routing: The possibility to change the routing in both the IP layer and the WDM layer intuitively offers the greatest opportunities for energy savings.

Extensive work on power-efficient networks has been done by the group of Prof. Tucker. [28] is especially relevant to our work. It tackles IP-over-WDM backbone transport networks with no OXC switching capability. The authors formulate a MILP to minimize power consumption of the network in two layers (router ports, transponders, and Erbium-doped Fiber Amplifiers can be switched off), and propose two heuristics for energy-efficient IP-over-WDM networks ("direct bypass" and "multi-hop bypass"). They consider three networks: a test network with 6 nodes and 8 links, the NSFNET network with 14 nodes and 21 links, and USNET with 24 nodes and 43 links. The heuristics are compared against the optimum solution and LP relaxed solution (for two smaller networks), and against "non-bypass" network (for all the networks). The relaxation of a MILP is

achieved by allowing all the integer variables to take real values. Assuming static, uniformly distributed random traffic and realistic power values for the considered networks, the authors conclude that the IP routers contribute the most to the power consumption of the network. Moreover, they point out that the power savings achieved by the lightpath bypass strategy increase with the network size, and that the power consumption distribution across the network nodes has a large variance for the "non-bypass" case, as opposed to the "direct bypass" and "multi-hop bypass". Eventually the authors note that minimizing energy and minimizing cost gives similar results in all the considered scenarios.

Yetginer and Rouskas [37] consider a two-layer architecture with each node equipped with an OXC and a DXC. Routing of lightpaths over the physical layer (fibers) and routing of traffic over the lightpaths are taken as variables in the proposed ILP. Following the metric proposed in [15], the authors of [37] define the power consumption of the network as a weighted sum of the number of lightpaths and total amount of traffic electronically routed. Three objective functions originate out of this metric: Minimum Number of Active Router Ports (minL), Minimum Amount of Electronically Switched Traffic (minT) and Minimum Power Consumption (minP). A 6-node network with 8 links under random traffic (uniform distribution with varied average value) is studied. The power consumption of a lightpath under no load (fixed power consumption) is equal to 0.25 of the power consumption of a lightpath under full load (maximum power consumption). The results indicate that minP uses only a few more lightpaths than minL. The difference between minP and minT in terms of electronically switched traffic vanishes as the network load is increased. Traffic dynamics over time is not discussed.

A trade-off between energy-efficiency and CAPEX minimization is studied by Palkopoulou et al. [29]. Two network architectures are considered: IP-over-WDM (IPoWDM) and IP-over-optical-transport-network-over-WDM (IPoOTNoWDM). Energy-efficiency is optimized (the optimization model is not presented in the paper) in the Germany17 network under random traffic (uniform distribution with varied maximum value, but no dynamics over time). Transport link failures and core router failures are taken into account. Cost values taken from [38] and power values according to internal Nokia Siemens Networks estimations apply. Transponders, router port cards and EXC port cards contribute to the power

consumption with the dominating contribution of the IP equipment. The investigations show that on a fixed network architecture and under changing load similar amount of energy is consumed network-wide no matter whether CAPEX minimizing approach or power minimizing approach is taken. The most cost-efficient architecture is not always the least energy consuming one under certain load though. The optimal architecture in terms of power consumption is dependent on the inter-node traffic demand. However, the relative power contribution of different network layers is independent of the average inter-node traffic demand for both IPoWDM and IPoOTNoWDM. A prediction on future power of network equipment is also made.

Routing in IP and optical layers is also considered by Shen et al. [39]. The ILP proposed by the authors has two objective functions, minimizing power or cost of the network. The same 6-node 8-link network as in [29] is considered. It is fed with random traffic (uniform distribution with varied maximum value). The same values for power [15] and cost are applied, with the only difference that each processed traffic unit consumes additional power, but contributes no costs. Energy can be saved by varying amount of the processed traffic, number of chassis, line cards and transponders equipped at a node. The authors show that multi-layer networks consume approximately 80% of the total power consumption of networks with no bypassing of routers (referred to as IP networks). The authors also show that the profit of diversified-volume lightpaths in terms of network power-efficiency against non-diversified-volume lightpaths decreases with increasing load. Eventually, the power-minimized network is shown to be more power-efficient than the cost-minimized network due to penalty for traffic processing. Dynamics of traffic over time is not taken into account.

Chowdhury et al. [40] compare Mixed-Line-Rate (MLR) networks with Single-Line-Rate (SLR) networks in terms of energy cost. They use a MILP which determines the number of installed fibers, the virtual topology and routing of traffic over the virtual topology. The physical routes of lightpaths are determined by Dijkstra's algorithm, however the link weights are not specified in the paper. Energy can be saved by varying the number of transponders, in-line amplifiers and amount of electronically processed traffic which increases power consumption. Using transponders of different rates (10, 40 and 100 Gbps) with power values unreferenced due to lack of space, the authors

show on the NSFNET network (14 nodes and 22 links) subject to unreferenced traffic matrix that MLR networks are more energy-efficient than the SLR ones. Moreover, they point out that correlation between CAPEX minimized and energy minimized networks depends on the CAPEX model. Influence of changing traffic demands over time on the energy savings is not discussed.

Our contribution: Various approaches to energy saving on different layers have been proposed so far in the literature. They all show that significant energy savings can be achieved, however it has been stressed in many papers that the presented MILPs are NP-hard, and therefore small networks considered or heuristics applied. Moreover, random traffic data and unreferenced power and cost values have been used in some papers. Our work extends the work presented above in that we consider and compare several rerouting strategies on different layers in the IP-over-WDM network (FUFL, DUFL, DUDL). We evaluate the potential energy savings using sophisticated mixed integer programming methods with time-varying traffic demands obtained from measurements in realistic networks, using realistic cost and power consumption values of the network equipment. We cover different time scales, temporal and spatial distribution of traffic, and demand scalings. We find solutions which are mostly optimal. Moreover, we have found no previous work which considers FUFL ([25] is the closest in the WDM layer).

4. Methodology and mathematical models

In the first step we design an IP-over-WDM network including the installation of fibers and all necessary hardware. This network serves as a basis for our investigations, and is considered to be *static* - it is independent of demand fluctuations over time, and all hardware equipment as well as the IP routing and the realization of lightpaths in the optical domain are fixed and powered on. Given this base network, we then compare the three approaches minimizing the number of active line cards.

4.1. Design of a base network

Designing a cost-minimal multi-layer network that allows to realize a given demand matrix is a highly complex problem which is far from being solved yet; see for instance [7, 20, 21, 22, 23]. The problem becomes even harder if multiple demand matrices are to be considered, leading to robust multi-layer network design problems [41, 42].

Most attempts to solve robust network dimensioning problems, however, assume single-layer networks; see [12, 13, 43] and references therein.

Given detailed traffic measurements, our approach is based on constructing a single demand matrix that refers to all peak demands over time. The base network is then dimensioned with respect to this maximum matrix which ensures that every single traffic scenario can be realized. The base network can be considered being cost-minimal among all networks that allow to route the constructed maximum demand matrix. Note that although common in practice, this approach is potentially producing overprovisioned networks. There might be cheaper topologies that cannot accommodate the maximum traffic matrix but all single traffic scenarios (with static IP routing). It is also typically unlikely to have all demands at their peak simultaneously. For our study, however, this approach based on a maximized matrix is reasonable since our main goal is to compare the three different energy saving concepts among each other rather than providing the cheapest among all robust base networks.

Let V be the set of all demand end-nodes and let $d_{ij}^{(t)}$ be the undirected demand value for each pair of nodes $(i, j) \in V \times V, i < j$ and each point in time $t \in T$. We compute the maximum demand matrix $(d_{ij})_{(i,j) \in V \times V}$ by

$$d_{ij} := \max_{t \in T} d_{ij}^{(t)}, \quad (1)$$

and calculate a minimum-cost IP-over-WDM network which satisfies this maximum demand matrix.

Our model used to cost-optimally design the base network is close to the one used in [6, 7, 22, 44, 45]. We optimize both network layers at the same time in an integrated step. The model comprises all relevant sources of installation cost both in the IP and the WDM layer. Extensions of this model are later used to evaluate the energy savings in different demand scenarios.

Parameters: Assuming all network elements to be bidirectional, we model the optical layer by an undirected physical supply network $G = (V, E)$ consisting of the nodes V and the physical links E . Every node $i \in V$ can be equipped with an IP router out of the set N of IP routers. Every router $n \in N$ has a maximum switching capacity of R^n and a cost of a^n . Every physical link $e \in E$ can operate an arbitrary number of fibers at cost β^e per fiber, each supporting B wavelength channels. For simplicity and due to the absence of realistic power data we do not consider different optical nodes to

be available. Instead we assume a pre-installed optical cross-connect (OXC) of infinite capacity at every network node. The model (2) can be easily extended by a physical node model though. Also note that we include some cost for OXCs in the cost of fibers; see Section 5.

For every node pair $(i, j) \in V \times V, i < j$, the set $P_{(i,j)}$ denotes all admissible routing paths in G between nodes i and j , which can be used to realize lightpaths. Let P be the union of all these paths and P_i the set of all paths ending at node i . Every path $p \in P$ can be equipped with multiple lightpaths of capacity C . Each bitrate unit C on a path p incurs the cost γ of line card interfaces at the end-nodes of p and consumes one wavelength channel in the physical network on every physical link of the path.

Demands and commodities: We assume that IP traffic can be arbitrarily split and routed via multiple virtual paths, as mentioned in Section 2. This is modeled by a standard so-called splittable multi-commodity flow [46] on the IP network layer. We remark that the main motivation behind this assumption is computational tractability since any more restrictive routing assumption (e.g. single-path flow or path length restrictions) would involve using discrete flow variables and/or additional flow constraints. From the practical point of view, we refer the reader to [47] for a discussion on the similarity of load distribution in a network using multi-commodity flows and a network using the OSPF (Open Shortest Path First) protocol with ECMP (Equal-Cost Multi-Path) routing and clever weight setting.

We introduce commodities based on the given point-to-point demands d_{ij} , $(i, j) \in V \times V, i < j$ in order to model a multi-commodity flow. There are mainly two approaches related to the definition of commodities [5, 46, 48, 49]. The first is to consider one commodity for every non-zero point-to-point demand. This approach results in the so-called disaggregated formulations which can become huge already for small networks. The number of variables and constraints in such models is in the order of $\mathcal{O}(|V|^4)$ and $\mathcal{O}(|V|^3)$, respectively, just for modeling the flow. For smaller models and to reduce computation times it is common to aggregate demands at common source nodes which leads to commodities having one source but several target nodes. This modeling trick reduces the number of commodities to at most $|V|$ and the number of variables and constraints in the multi-commodity flow model to $\mathcal{O}(|V|^3)$ and $\mathcal{O}(|V|^2)$, respectively.

In the following the set of commodities $K \subseteq V$ corresponds to those nodes in V that are source of

at least one demand. For commodity $k \in K$ and every node $i \in V$ we define the net demand value

$$d_i^k := \begin{cases} \sum_{j \in V} d_{ij} & \text{for } i = k \\ -d_{ki} & \text{otherwise} \end{cases}.$$

With this definition we subsume all demands whose source is $k \in V$. It holds that $\sum_{i \in V} d_i^k = 0$ for all $k \in K$. The total demand value d_i of a network node i is given by the sum of all demands having its source or target in i , that is, $d_i := \sum_{k \in K} |d_i^k|$.

Variables: The flow variables $f_{ij}^k, f_{ji}^k \in \mathbb{R}_+$ describe the flow for commodity k on the virtual link between i and j in both directions. Notice that the flow variables are not defined for individual lightpaths. The variables aggregate the IP traffic on all lightpaths with end-nodes i and j . This is possible because the actual physical representation of a virtual link does not matter for the IP routing. Only the total capacity between any two nodes is of interest for an IP demand in our model. Also notice that by the definition of the commodities above the flow variables aggregate IP traffic with the same source node. The distribution of virtual link flow to the chosen physical representations and also the disaggregation of the commodity flows to individual demand flows can be done in a postprocessing step, as explained below and in [22, 44]. Both aggregation techniques significantly reduce the size of the model compared to considering flow variables on individual physical representations and for individual point-to-point demands.

Variables $y_p \in \mathbb{Z}_+$ count the number of lightpaths realized on $p \in P$. Similarly, $y_e \in \mathbb{Z}_+$ denotes the number of fibers installed on physical link $e \in E$. The binary variable $x_i^n \in \{0, 1\}$ states whether or not router n is installed at node $i \in V$.

Model: The problem of minimizing the cost for a feasible network configuration and routing satisfying the demand matrix d can be formulated as the MILP (2). Equations (2a) are the flow conservation constraints for every node and commodity, formulated on the complete virtual layer $V \times V$. Inequalities (2b) choose a subset of paths between the nodes i and j and install enough capacity to accommodate all the virtual link flow corresponding to (i, j) . The virtual node capacity constraints (2c) make sure that the capacity of a node suffices to switch all the incoming traffic, including the emanating demand. Constraints (2d) select one router configuration at every node. Eventually, the physical link capacity constraints (2e) make sure that the number of available wavelengths on a fiber is not

exceeded.

$$\min \sum_{i \in V, n \in N} \alpha^n x_i^n + \gamma \sum_{p \in P} y_p + \sum_{e \in E} \beta^e y_e$$

$$\sum_{j \in V \setminus \{i\}} (f_{ij}^k - f_{ji}^k) = d_i^k, \quad i \in V, k \in K \quad (2a)$$

$$\sum_{p \in P_{(i,j)}} C y_p - \sum_{k \in K} (f_{ij}^k + f_{ji}^k) \geq 0, \quad (i, j) \in V \times V \quad (2b)$$

$$\sum_{n \in N} R^n x_i^n - \sum_{p \in P_i} C y_p \geq d_i, \quad i \in V \quad (2c)$$

$$\sum_{n \in N} x_i^n \leq 1, \quad i \in V \quad (2d)$$

$$B y_e - \sum_{p \in P: e \in p} y_p \geq 0, \quad e \in E \quad (2e)$$

$$f_{ij}^k, f_{ji}^k \in \mathbb{R}_+, \quad y_p, y_e \in \mathbb{Z}_+, \quad x_i^n \in \{0, 1\} \quad (2f)$$

The flow for commodities $k \in K$ on virtual link $(i, j) \in V \times V$ has to be disaggregated in two steps in postprocessing. First, we have to disaggregate the flow from the virtual links (i, j) to all physical representations $p \in P$ with end-nodes i and j (in both directions). By (2b) this can be done respecting the installed capacities $C \cdot y_p$ for $p \in P_{(i,j)}$. Let f_p^k denote the flow on path p for commodity $k \in K$. In a second step, the commodity flow f_p^k has to be disaggregated to a flow for every individual point-to-point demand $(i, j) \in V \times V$, where i corresponds to the source of commodity k and j to one of its targets. Since commodities have been aggregated from demands at common source nodes, this can be done in a greedy manner by iteratively subtracting the necessary individual demand flow for every target j from the given aggregated commodity flow. We denote by $f_p^{(i,j)}$ the flow for demand (i, j) with value d_{ij} on path p .

4.2. Evaluation of different demand scenarios

In the following, we explain how we adapt model (2) to evaluate the possible energy savings for FUFL, DUFL and DUDL under dynamically changing demands. The complete model variants (DUFL and DUDL) are presented in the Appendix A. The notation for all models and the postprocessing steps is summarized in Table 1. For all approaches we fix the physical network by fixing the variables y_e to the values y_e^{base} from the static base network. We also fix the variables x_i^n of the installed IP routers together with all installed line cards at each node $i \in V$ according to the base network solution. The capacity of the IP router installed at node i is denoted by R_i^{base} .

FUFL : Consider a demand between nodes i and j with base value d_{ij} . In each low-demand hour $t \in T$ where this demand has value $d_{ij}^{(t)}$, we reduce the flow on each path p used to transport this demand by the factor $d_{ij}^{(t)}/d_{ij} \in [0, 1]$ and reduce the capacity on the path accordingly. As all flows for this demand are scaled by the same factor, the relative share of traffic on each used path remains the same as before.

To state it more precisely, consider a path p used to route demand d_{ij} . In scenario $t \in T$, we reduce the flow from $f_p^{(i,j)}$ to

$$f_p^{(i,j)^{(t)}} := f_p^{(i,j)} \cdot d_{ij}^{(t)}/d_{ij}.$$

Let

$$f_p^{(t)} := \sum_{(i,j) \in V \times V} f_p^{(i,j)^{(t)}}$$

be the total flow on path p after reducing the flow for all demands. Then the capacity on that path can be reduced from y_p^{base} to

$$y_p^{(t)} := \left\lfloor \frac{f_p^{(t)}}{C} \right\rfloor,$$

where y_p^{base} is the capacity of the virtual link p in the base network. Remember that variables y_p count the number of lightpaths on $p \in P$. Hence this procedure corresponds to shifting traffic between parallel lightpaths, that is, lightpaths with the same realization $p \in P$. No optimization is needed. From a practical perspective alternative FUFL principles might be of interest. Traffic could be shifted between all paths $p \in P$ having the same end-nodes (i, j) ignoring physical representations. This could reduce the number of active lightpaths even more and completely relies on information available at the IP layer. Additionally adjusting the splitting of demands across IP multi-paths could further contribute to energy savings. For ease of exposition we neglect to study these FUFL variants here.

DUFL : For every $t \in T$, we compute a new IP routing by using a variant of model (2). The virtual link capacity variables y_p can be reduced compared to the base network, but not augmented. This is ensured by adding the constraint $y_p \leq y_p^{base}$ to (2) for all $p \in P$. The IP flow can be rerouted without any further restrictions such as to minimize the number of active line cards. Hence an energy optimal routing for every time period $t \in T$ can be computed by fixing and bounding variables y_e , x_i^n and y_p in (2) as described above, using the demand matrix $d^{(t)}$ instead of d , and changing the objective function to

Table 1: Notation used in the MILPs and postprocessing steps

| Symbol | Description | | |
|-----------------|---|--|--|
| $G = (V, E)$ | undirected physical supply network with nodes V and physical links E | | |
| $P_{(i,j)}$ | set of all admissible paths in G between nodes i and j | | |
| P | set of all admissible paths in G , that is, $P := \cup_{(i,j) \in V \times V} P_{(i,j)}$ | | |
| P_i | set of all admissible paths ending at node i , that is, $P_i := \cup_{j \in V} P_{(i,j)}$ | | |
| N | available set of IP routers | | |
| R^n | switching capacity of router $n \in N$ | | |
| α^n | cost of router $n \in N$ | | |
| B | capacity of a fiber in terms of supported wavelengths | | |
| β^e | cost of a fiber installed at physical link $e \in E$ (length dependent) | | |
| C | capacity (bitrate) of a lightpath | | |
| γ | cost of a lightpath (based on the cost of line card interfaces at both ends) | | |
| K | set of commodities, corresponding to all source nodes in V | | |
| T | set of considered points in time (time periods) | | |
| $t \in T$ | $d_{ij}^{(t)}$ | demand value with source i and target j (at time $t \in T$) | |
| | $d_i^{k(t)}$ | net demand value for commodity $k \in K$ and node $i \in V$ (at time $t \in T$) | |
| | $d_i^{(t)}$ | total demand value of node $i \in V$ (at time $t \in T$) | |
| peak | d_{ij} | demand value with source i and target j (max over time) | |
| | d_i^k | net demand value for commodity $k \in K$ and node $i \in V$ (max over time) | |
| | d_i | total demand value of node $i \in V$ (max over time) | |
| Variables | $f_{ij}^k, f_{ji}^k \in \mathbb{R}_+$ | flow for commodity k between nodes i and j (in both directions) | |
| | $y_p \in \mathbb{Z}_+$ | number of lightpaths realized on path $p \in P$ | |
| | $y_e \in \mathbb{Z}_+$ | number of fibers installed on physical link $e \in E$ | |
| | $x_i^n \in \{0, 1\}$ | decides whether to install router n at node $i \in V$ or not | |
| Solution Values | Base | y_p^{base} | number of lightpaths realized on path $p \in P$ in the base network |
| | | y_e^{base} | number of fibers installed on physical link $e \in E$ in the base network |
| | | R_i^{base} | capacity of IP router installed at node $i \in V$ in the base network |
| | | f_p^k | flow on path $p \in P$ for $k \in K$ in the base network, computed from f_{ij}^k, f_{ji}^k |
| | | $f_p^{(i,j)}$ | flow on path $p \in P$ for demand (i, j) in the base network, computed from f_p^k |
| FUFL | $f_p^{(i,j)(t)}$ | reduced flow on path $p \in P$ for demand (i, j) at time $t \in T$ | |
| | $f_p^{(t)}$ | total reduced flow on path $p \in P$ at time $t \in T$ | |
| | $y_p^{(t)}$ | reduced capacity on path $p \in P$ at time $t \in T$ | |

minimize the number of active lightpaths $\sum_{p \in P} y_p$. The detailed model (A.1) to reoptimize the routing in every time step using the strategy DUFL can be found in the Appendix A.

DUDL : We are allowed to change the IP routing as well as the virtual topology including physical representation of the lightpaths. But we cannot install new line cards at IP routers. Similarly to DUFL, we use a variant of model (2) to compute an energy-efficient network in each demand scenario $t \in T$. In contrast to the previous case, the augmentation of virtual link capacity variables y_p is allowed in addition to changing the flow variables. In order not to exceed the number of line cards installed at each node in the base network, we add the constraints

$$\sum_{p \in P_i} y_p \leq \sum_{p \in P_i} y_p^{base}$$

for every node $i \in V$. We then minimize the number of used line cards for every demand scenario using the same objective as for DUFL; see model (A.2) in the Appendix A.

5. Data

We have made an effort to use as realistic data (network topologies, traffic demands, costs, and power) as possible. We have used the detailed hardware and cost model for IP and WDM equipment from [38], which has been developed by equipment vendors and network operators within the European NOBEL project [50]. Traffic data originates from measurements and determines network topologies, as reported further on in this section. Our energy evaluations are based on the model presented in [27].

Cost and power of network elements In the following we briefly describe the network elements we used to design the IP-over-WDM architecture (see Fig. 1(b)). Every network node can be equipped with one out of 13 different IP routers accommodating 16–208 line cards with a capacity of 640–8320 Gbps. Routers with a capacity of more than 640 Gbps are multi-chassis configurations incurring a multi-chassis setup cost such that the cost for the smallest router with 16 slots is $\alpha^1 = 16.67$ and for the remaining 12 routers with 32 to 208 slots it roughly holds that $\alpha^i = 111.67 + (i-2) \cdot 29.17$ with $i \in \{2, \dots, 13\}$; also see [38].

We considered a 40 Gbps colored line card interface that connects the IP router to the WDM system. To estimate the cost of this interface following [38], we combined a 40 Gbps IP router slot card, a

4x10 GE port card, and a 4x10G ELH muxponder at Nobel-cost of 19.42. A lightpath is set up using these interfaces at both ends of the path, hence $\gamma = 38.84$. The power was evaluated by combining a Cisco 4-port 10-GE Tunable WDM PHY PLIM and a Modular Services Card which together consume 500 W [14, 27] and hence 1000 W for a single lightpath.

We assume an 80-channel optical system. Following [38], an optical fiber installed on a physical link is composed of optical line amplifiers (OLA), dynamic gain equalizers (DGE), dispersion-compensating fibers (DCF), and WDM multiplexers. As in [38] we assume an OXC to be composed of wavelength-selective switches (WSS), which results in a fixed cost and a cost that linearly scales with number of connected fibers. We may hence map the latter to the cost of fibers. The corresponding total cost β^e of a fiber depends on the length of the actual physical link. In our case it holds that $\beta^e \in [21.16, 31.83]$, $\beta^e \in [24.67, 179.16]$, and $\beta^e \in [20.85, 134.63]$ for the networks Germany17, Géant, and Abilene, respectively.

Network topologies We used three physical supply network topologies as depicted in Fig. 3. The German backbone network Germany17 with 17 nodes and 26 links (Fig. 3 (a) and (b)) has been defined as a reference network in the NOBEL project [50]. The Abilene network (12 nodes and 15 links, Fig. 3(c)) is an American network commonly used in the research community [51]. The largest network we investigated (22 nodes and 36 links, Fig. 3(d)) is the pan-European research network Géant, which connects European National Research and Education Networks (NRENs) [52]. Other than in the original data, we treated two German nodes as one in Géant due to location problems.

Considering each single network we precalculated the set $P_{(i,j)}$ of the 50 shortest paths for potential lightpaths for every node pair (i, j) . The length of a physical link was computed by using the spherical distance of its end-nodes. The paths were limited in total physical link length to 3000 km. There are three physical links in the Géant network with a real length greater than 3000 km (Israel–Netherlands, New York–Austria and New York–UK). We set these links to a length of exactly 3000 km. There is thus only the direct path possible between these nodes. This way we implicitly assume to provide the necessary regenerators on these three links at no cost.

Traffic demands The choice of the network

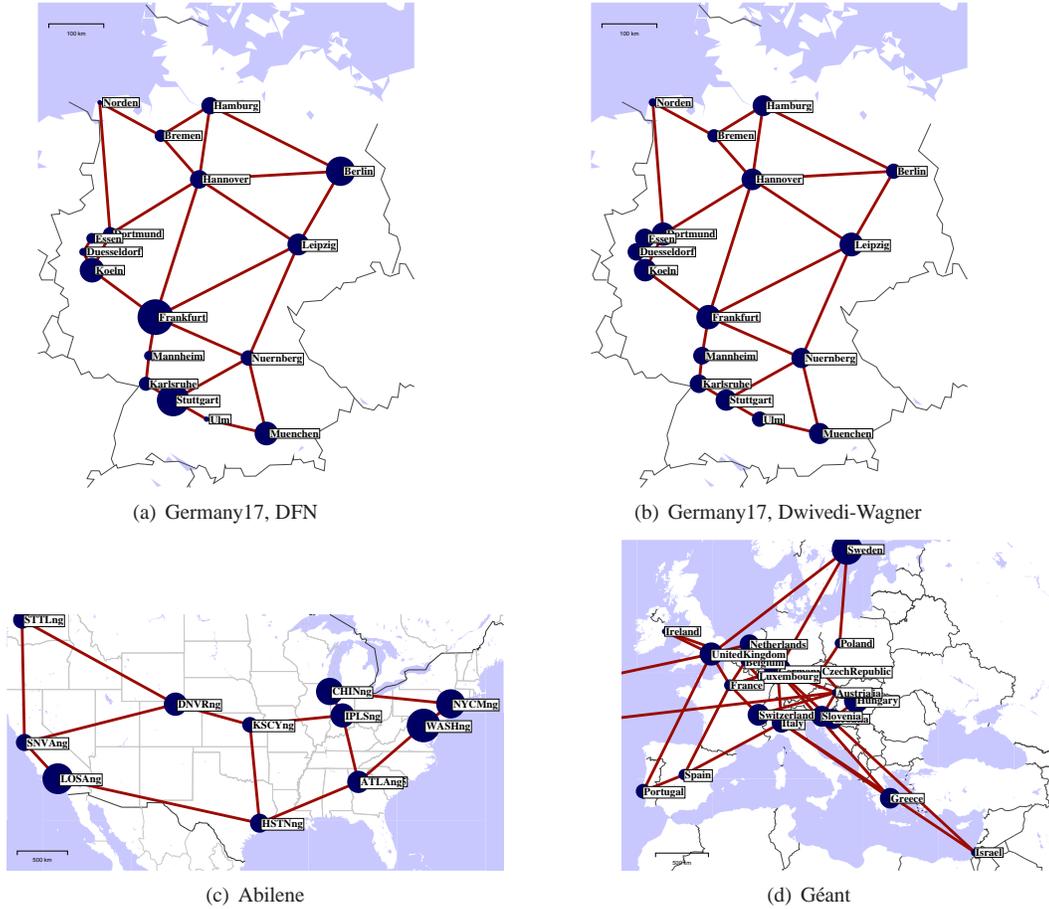


Figure 3: Physical supply network topology, and source traffic distribution. The area of a node represents its emanating demand. The DFN demands (a) are Frankfurt-centralized in contrast to the DWG demands (b). Notice that the New York node is omitted in the Géant figure (c).

topologies presented above was dictated by the limited availability of traffic measurements. To vary the ratio between demands and the capacity granularity, we scaled all demands by the same factor such that the sum $\sum_{i<j} d_{ij}$ of all demands in the maximum demand matrix was 1 Tbps, 3 Tbps or 5 Tbps. We refer to these values as the *maximum total demand*, while the value $\sum_{i<j} d_{ij}^{(t)}$ denotes the *total demand* at time $t \in T$.

One set of dynamic demands (for Germany17) was taken from measurements in the year 2005 in the national research backbone network operated by the German DFN-Verein [53], see Fig. 4 (a), Fig. 5 (a), and Fig. 5 (b). The original DFN data consists of the total end-to-end traffic in bytes every 5 minutes over the day 2005-02-15, every day of February 2005, and every month over the year 2005. According to our partners at DFN-Verein, the traffic patterns in these periods were rather representative. We aggregated the 5-minute traffic ma-

trices to 15-minute traffic matrices by taking the maximum value for each demand over the whole aggregation interval (in contrast to [1]). Eventually all matrices were mapped from the original DFN locations to the Germany17 network according to the smallest geographical distances.

A different set of traffic matrices was used for the Abilene network. It originates from the Abilene Observatory [54] and is available at [51]. The original data of 5-minute time granularity has been aggregated to similar time intervals as for the DFN measurements (the whole year could not be covered due to data unavailability - we considered time intervals of 2 weeks between 2004-05-01 and 2004-07-24 instead). The traffic with 15-minute intervals over 2005-05-08 is shown in Fig. 4 (c).

Traffic matrices based on measurements in the Géant network [52] have been made available to us. They were collected using Netflow statistics and BGP Routing Information Base (RIB). We consider

Table 2: Network topologies and traffic

| Network | Nodes | Links | Time granularity | Reference |
|-----------|-------|-------|--|-------------|
| Abilene | 12 | 15 | every 15 min. of 2004-05-08, every day of 2004-05, every two weeks between 2004-05-01 and 2004-07-24 | [51] |
| Géant | 22 | 36 | every 15 min. over a day, every day over a month | [52] |
| Germany17 | 17 | 26 | every 15 min. of 2005-02-15, every day of 2005-02, every month of 2004 using DFN-measurements and Dwivedi-Wagner model | [8, 50, 53] |

traffic matrices with the original time granularity of 15 minutes over a day (Fig. 4 (d)), and time intervals of a day over a month.

The traffic values for all networks have been converted to Mbps and scaled to obtain comparable maximum total demand values (1 Tbps, 3 Tbps and 5 Tbps). To get undirected demands between nodes i and j we considered the maximum of the two corresponding directed demands.

As shown in Fig. 3 (a), the DFN matrices have a centralized structure with a large demand emanating from Frankfurt, which is a large entry point for cross-atlantic traffic; see [6]. They also exhibit temporal peaks caused by single academic institutions sending large amounts of traffic to another institution or to an international backbone. Therefore we also evaluated the energy savings in Germany17 with demand matrices generated using the Dwivedi-Wagner (DWG) model [8] based on population statistics. The resulting demands are much less centralized (compare Fig. 3 (a) and (b), the area of each node is proportional to its emanating demand). The DWG model distinguishes between data, voice, and video traffic and computes demand values between two cities according to their distance and their number of inhabitants, employees, or households depending on the traffic class. From the single demand matrix $(b_{ij})_{(i,j) \in V \times V}$ obtained from the DWG model, we generated demand matrices for all time periods by applying the relative demand changes in the DFN measurements to the computed DWG matrix as follows. Given the DFN demands $d_{ij}^{(t)}$ over time, the maximum DFN demands d_{ij} , and the static DWG demands b_{ij} , we calculate dynamic DWG demands $b_{ij}^{(t)}$ in the following way:

$$b_{ij}^{(t)} := b_{ij} \cdot d_{ij}^{(t)} / d_{ij}.$$

The time-dependent scaling factor $d_{ij}^{(t)} / d_{ij}$ takes values in the interval $[0, 1]$ normalizing the maximum DFN demand for every (i, j) . It hence rules

out the domination effects caused by single demands in the measurements. Fig. 5 illustrates this effect for the daily total demand values over a month (a), and monthly total demand values over a year (b). The topologies and traffic data are summarized in Table 2.

6. Results

This section describes our computational results on the data presented in the previous section. We first explain the essence of our results using the Germany17 network and the 96 DFN traffic matrices given for every 15 minutes of 24 hours, and discuss these results in detail. Thereafter, we illustrate that for DUFL and DUDL these results are invariant against changes of

- the ratio between demand values (scaled to 1, 3 and 5 Tbps maximum total demand) and the capacity granularity (40 Gbps lightpath bitrate),
- the network (Germany17, Abilene, and Géant),
- the time scale of the demands (every 15 minutes over a day, every day over a month, and every month over a year), and
- the structure and spatial distribution of the demand matrix (DFN measurements or Dwivedi-Wagner model using population statistics).

while we report on the influence of the maximum total demand and the spatial distribution of traffic (measurements versus population statistics) on the success of FUFL. All occurring MILPs have been solved using CPLEX 12.1 [55] as a black-box solver with a time-limit of one hour on a 64-bit Intel 3.00 GHz CPU with 8 GB main memory. The size of the MILPs to compute the base network in

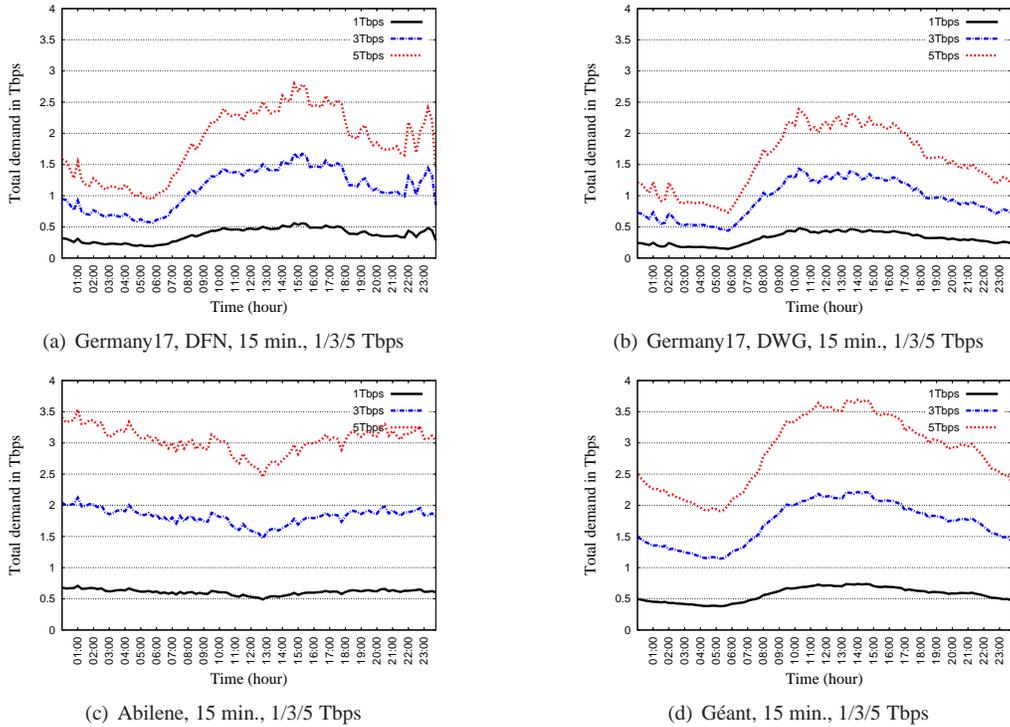


Figure 4: Total demand over a day in Tbps for the scenarios with 1/3/5 Tbps maximum total demand. The traffic shows different levels of dynamics. The Germany17 (a), (b) and Géant demand (d) shows a typical day/night pattern with more short-range dynamics for Germany17. The Abilene demand (c) is quite flat over the day.

Table 3: Size of the MILPs to compute the base network in terms of variables and constraints. Simple upper or lower bound constraints for variables are not counted.

| Network | variables | | | constraints |
|-----------|-----------|----------------|----------------|-------------|
| | bin | \mathbb{Z}_+ | \mathbb{R}_+ | |
| Abilene | 156 | 87 | 1452 | 237 |
| Germany17 | 221 | 6559 | 4352 | 468 |
| Géant | 286 | 3006 | 9702 | 773 |

terms of variables and constraints is presented in Table 3. These correspond to the size of model (2). Notice that the size of the models (A.1) and (A.2) cannot be explicitly stated since it very much depends on the concrete solution for the base network. The number of variables however is always reduced since the variables for IP routers and fibers are fixed. For DUFL even most of the path-variables can be omitted if the paths are not used in the base network solution. Also the number of constraints in (A.1) and (A.2) is bounded from above by the number of constraints in (2). We do not count simple bound constraints such as non-negativity constraints or (A.1d).

6.1. Results for the Germany17 network with DFN matrices over one day

We could compute an energy-minimal solution within seconds or minutes for most of the DUFL scenarios on the Germany17 network with the 15-minute DFN matrices for a day. For only a few instances we hit the time-limit with an optimality gap (relative difference between the number of line cards in the best solution and a mathematically proven lower bound to this number) below 5%. The optimization problem corresponding to DUDL is harder to solve. All DUDL runs hit the time-limit with optimality gaps of 11%–30% (1 Tbps), 6%–25% (3 Tbps), and 3%–15% (5 Tbps). A higher relative optimality gap for DUDL can be observed for the 1 Tbps maximum total demand than for 5 Tbps. All comparisons of the three strategies are made against the lower bound on the number of line cards in use, which corresponds to an upper bound on the maximum possible energy savings in the considered scenario. Note that there are no dual bounds for FUFL since no optimization is performed with this approach. For almost all DUFL runs dual bounds and primal solution values are identical, which means that the computed

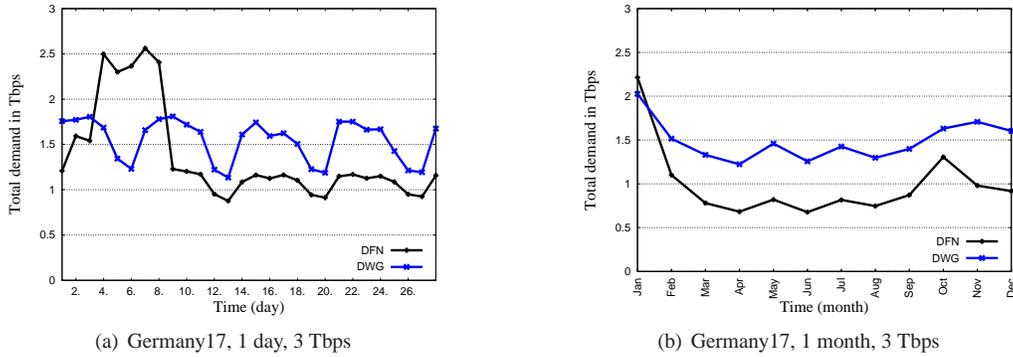


Figure 5: Total demand over time in Tbps for the scenario with 3 Tbps maximum total demand, every day of February 2005, and every month of 2004. The DWG matrices show the expected behavior over time with peaks during the week, low traffic on weekends (a), and a slightly rising demand over the year (b). In contrast, the DFN measurements exhibit peaks caused by single demands.

solutions are optimal. In the following figures we hence removed the dual bound for DUFL since it cannot be distinguished from the (primal bound) solution curve. Whenever reporting on power values we consider the total power consumptions of all active line cards assuming a value of 500 W for every single line card as explained in Section 5.

Fig. 6 illustrates the (close to) optimal power consumptions obtained with FUFL and DUFL as well as the power consumptions and dual bounds for DUDL for each of the three demand scalings. All the proposed approaches make use of the dynamics of traffic and follow the total demand curve (compare with Fig. 4(a)). The energy savings achieved with DUFL and DUDL are nearly identical and much larger than with FUFL. The flexibility of DUFL to reroute traffic saves a significant amount of energy compared to FUFL. In contrast, reconfiguring the virtual topology in the physical layer (DUDL) does not give much additional profit. In the 5 Tbps scenario the DUFL and DUDL curves nearly coincide. The lower bound for DUDL proves that only a small amount of energy can be saved compared to DUFL. There seems to be more tolerance in the 1 Tbps scenario. In this case we cannot verify whether our DUDL solutions are optimal or whether solutions closer to the lower bound exist. The constant periods of power consumption in Fig. 6(a) correspond to the minimal number of line cards that are needed to maintain IP connectivity.

More precisely, in the 1 Tbps scenario, the line cards of the network consume 0.89/0.75/0.50/0.38 MWh over the day for Base/FUFL/DUFL/DUDL, respectively. The corresponding values for 3 Tbps and 5 Tbps are 2.11/1.52/0.94/0.82 MWh and 3.29/2.15/1.36/1.28 MWh. Notice that these

values correspond to the power consumption of a single day. Accumulating these values over a year (multiplying by 365) results in power consumption of 1201/785/496/467 MWh over the year in the 5 Tbps scenario.

Although we focus on the comparison of the FUFL, DUFL and DUDL approaches, it may be interesting from the practical perspective to evaluate the energy savings against the static base network. One should however not overestimate these savings since the base network may be overprovisioned (peak demands typically do not occur simultaneously). In the 3 Tbps scenario FUFL reduces the power of the active line cards in low-demand hours by up to 38% at 05:30 am (72% for DUFL and 77% for DUDL). Even in a high-load scenario the savings are significant (17%, 39%, and 44% for FUFL, DUFL and DUDL at 02:45 pm, respectively). Considering the power consumption at 05:30 am and 02:45 pm for a maximum total demand of 3 Tbps, 25% of power for FUFL, 55% for DUFL, and 59% for DUDL can be saved in the early morning compared to the peak hour.

We observe that already the easy-to-realize FUFL saves substantial energy. The savings however depend on the ratio of the maximum total demand and the capacity of a single WDM channel C . If this ratio is low (traffic demands are low compared to a coarse lightpath bitrate) there is little potential to save energy with FUFL since a single lightpath might be sufficient to transport demands between pairs of nodes. Such single lightpaths cannot be switched off without the flexibility of IP rerouting – IP connectivity has to be maintained also in very low-demand hours. On the other hand if the demands are very large there are potentially many active lightpaths serving the same pair of nodes. The

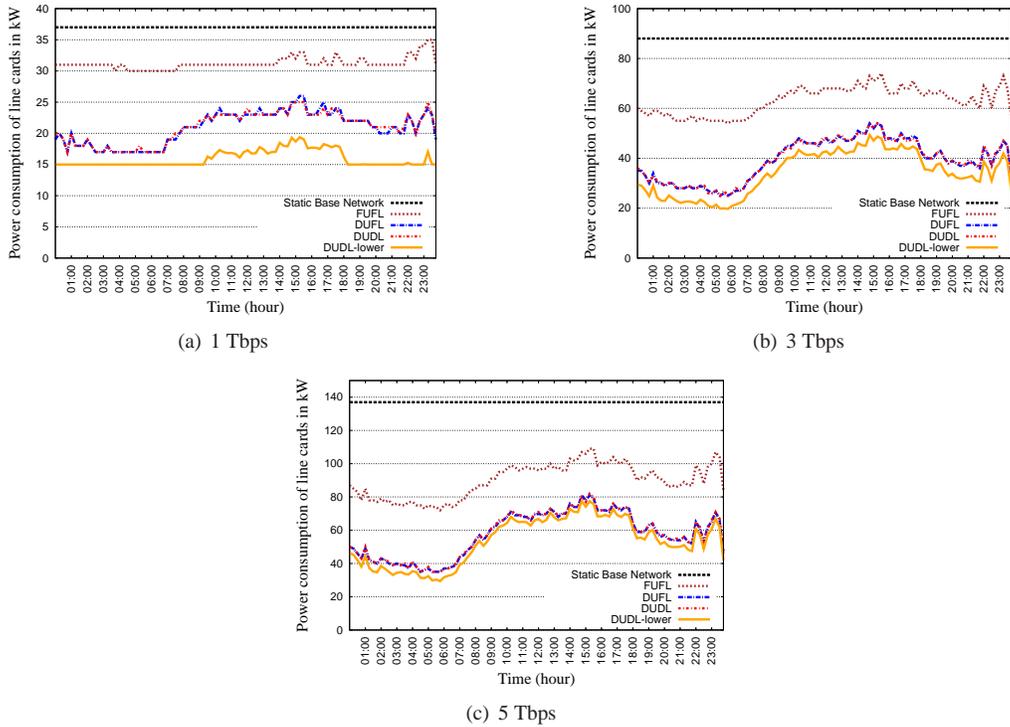


Figure 6: The figures show the power consumption in kilowatt with the three strategies on the Germany17 network, DFN traffic, 1/3/5 Tbps, every 15 minutes on February 15, 2005. The difference between FUFL and DUFL is much larger than the additional benefit of DUDL. Note that the y-axes are not identical.

traffic on such a virtual link is likely to drop below the 40 Gbps (80 Gbps, 120 Gbps, ...) threshold. It follows that with a constant bitrate of 40 Gbps for the line cards and increasing demands (from 1 Tbps to 5 Tbps) the relative outcome of FUFL increases which can be observed in Fig. 6(a) - (c). Compare also Fig. 9(a) with 9(c) and Fig. 9(b) with 9(d).

For a low-demand hour at 05:30 am in the 5 Tbps scenario, Fig. 7(a) - (d) show the virtual topologies corresponding to the base network and the considered approaches FUFL, DUFL, and DUDL, respectively. Although FUFL allows to reduce the link capacity (number of active line cards), the virtual topology remains nearly the same because existing virtual links have to be maintained even for small amount of traffic. In contrast, the virtual topology changes significantly with DUFL and DUDL. Moreover, lightpaths in DUFL and DUDL are highly utilized, as opposed to FUFL; see Fig. 8. Remember that DUFL may only use virtual links that exist in the base network in contrast to the energy saving scheme DUDL which may set up new lightpaths (e.g. Hannover–Norden, compare Fig. 7(a) and (d)). Nevertheless the virtual topologies of DUFL and DUDL are very close to each other with a sim-

ilar number of active line cards.

To understand the relatively poor outcome of DUDL, one has to consider two extreme scenarios. If the demand in the network is very large, the virtual topology in the base network is close to a full mesh (see Fig. 7(a)). Since DUFL may use any virtual link from the base network, the DUFL solution is (close to) optimal and DUDL cannot benefit from choosing lightpaths not existing in the base network. If, on the other hand, the demands are very small, the optimal virtual topology of the base network will be a tree. Both DUFL and DUDL will find a tree network. These trees might differ, but they use the same number of line cards. Again DUDL cannot benefit compared to DUFL. For the success of DUFL it is also crucial that we allow splitting of traffic demands in the virtual domain, which lets DUFL fill up the established lightpaths to a high extent. This is illustrated in Fig. 8(a) and Fig. 8(b). Moreover, the lack of power-hungry network elements in the WDM layer [28] leads to the lack of potential to save energy by rerouting of lightpaths.

6.2. Varying input parameters

To make sure that the observed results do not depend on specific assumptions on the network or the

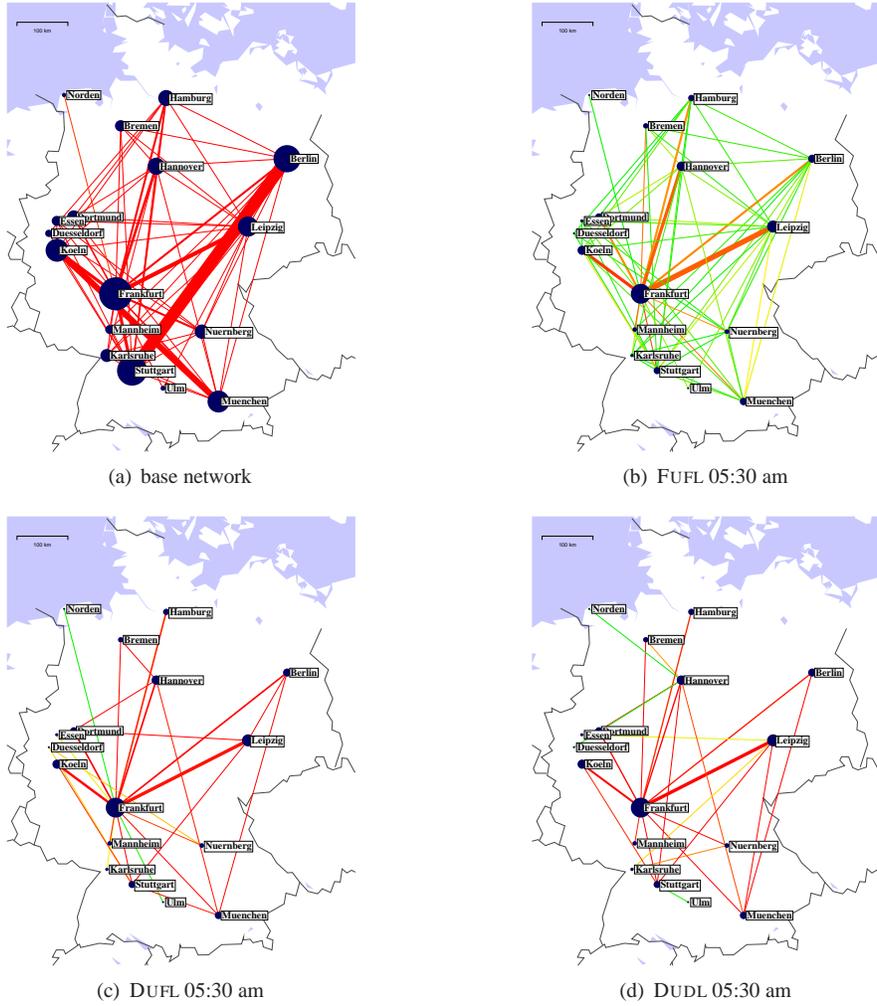


Figure 7: Virtual topologies of the base network and of the computed solutions with FUFL, DUFL, and DUDL at 05:30 am for the Germany17 network with DFN measurements, maximum total demand 5 Tbps. The color of a link corresponds to the load (high (red) and low (green)). The width of a link refers to its capacity. The size of a node represents its emanating demand.

input data we evaluated the performance of FUFL, DUFL, and DUDL for various parameter combinations of the network, the time scale, and the demand scalings and patterns. Since the observed results were basically consistent over all these scenarios, we show an example diagram for each of the variations. In the previous section, we have already shown that our results are nearly invariant against variations of the ratio between the demand and the capacity granularity, compare Fig. 6(a) - (c).

Varying the network: Second, we varied the network topology by using the traffic measurements on the Géant and Abilene networks described in Section 5. Fig. 9 shows the power consumption curves over time for these two networks. The difference in the outcome of the three approaches is similar to the results observed for Ger-

many17. The success of FUFL depends on the size of the demands while DUFL performs constantly well with almost no additional benefit by using DUDL. Notice that with the Abilene network, all obtained network topologies and power consumption values are optimal.

Varying the time scale: Third, we varied the time scale, which changed the structure of the demand variations over time. For the DFN measurements on the Germany17 network, we not only considered the 15-minute demand matrices over a day, but also aggregated measurements for every day over a month, and for every month over a year, as explained in detail in Section 5. Fig. 10 shows the power consumption over time with FUFL, DUFL, and DUDL for the latter two time scales on the Germany17 network with DFN de-

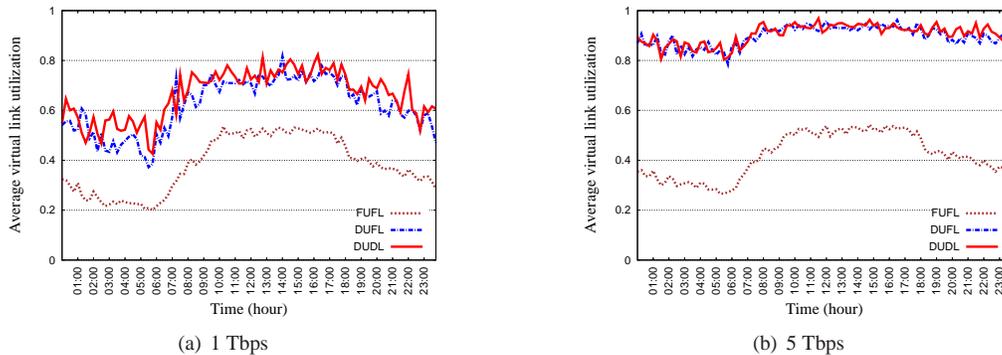


Figure 8: Average virtual link utilization over all active virtual links, Germany17, DFN, every 15 minutes. DUDL and DUFL achieve high lightpath utilization in contrast to FUFL.

mands. One can see that DUFL and DUDL are very close to each other and can save much more energy than FUFL also on these time scales.

Varying the demand pattern: Eventually, we varied the structure of the demands by using demands generated with the Dwivedi-Wagner (DWG) model instead of the DFN measurements. Fig. 11 shows the power consumption over time with the DWG demands on the Germany17 network. It turns out that the essential result does not change. The benefit of DUFL compared to FUFL is very large, and DUFL and DUDL differ only marginally. The plotted dual bounds show that the network topologies obtained in each time slot are close to the optimum. In particular, this shows us that this effect is due to structural differences of the considered rerouting concepts and not the result of some heuristic solution procedure.

On the other hand, it can be seen that the power reduction compared to the base network using the FUFL approach is marginal, which is in contrast to the results for the DFN demands (compare Fig. 6(b) with Fig. 11). Recall that the DFN traffic is very centralized with a large concentration of demand in Frankfurt, while the DWG demands are more evenly distributed (compare Fig. 3(a) with Fig. 3(b)). This has mainly two consequences. First, the line cards are more evenly distributed among the nodes in the 3 Tbps DWG solution with a minimum of 2 line cards (Norden) and a maximum number of 15 line cards (Frankfurt, Leipzig, and Muenchen) compared to a minimum of 1 (Norden and Ulm) and a maximum of 32 (Frankfurt) in the 3 Tbps DFN base network solution. And second, the number of used physical paths is larger in the DWG solution compared to the DFN solution, which influences the number of parallel lightpaths. In the DWG base network 87 physical paths are in

use with a maximum number of 2 lightpaths using the same physical path. The DFN solution uses a total of 50 paths with a maximum of 14 channels on the same path. Note however that the total number of lightpaths in use is almost the same in both scenarios (88 for DFN and 89 for DWG), because the sum of all demands is identical (3 Tbps). Since FUFL, as explained in Section 4, may switch off line cards only in the presence of parallel channels, the power consumption can only slightly be reduced with DWG demands. Here the spatial distribution of the traffic influences the impact of FUFL approach on energy saving. In contrast, we do not observe any differences for DUFL and DUDL.

7. Conclusions

Our study has shown that a significant amount of energy can be saved by switching off line cards in low-demand hours with any of the considered reconfiguration strategies FUFL, DUFL and DUDL. The formulated MILP allowed us to provide high quality estimates together with upper bounds on the maximum possible energy savings in the corresponding multi-layer optimization problems. We used realistic topologies, traffic data, cost and power values.

Summary of results: The main result is that rerouting demands in the IP layer (DUFL) contributes the most to the energy savings. Allowing additional reconfiguration in the optical domain (DUDL) barely brings any extra benefit in the considered scenarios. Extensive computational studies strongly suggest that these results are independent of the ratio between the demand and capacity granularity, the demand structure, the time scale, and the network topology. Already a simple monitoring of the traffic and downscaling the line card usage

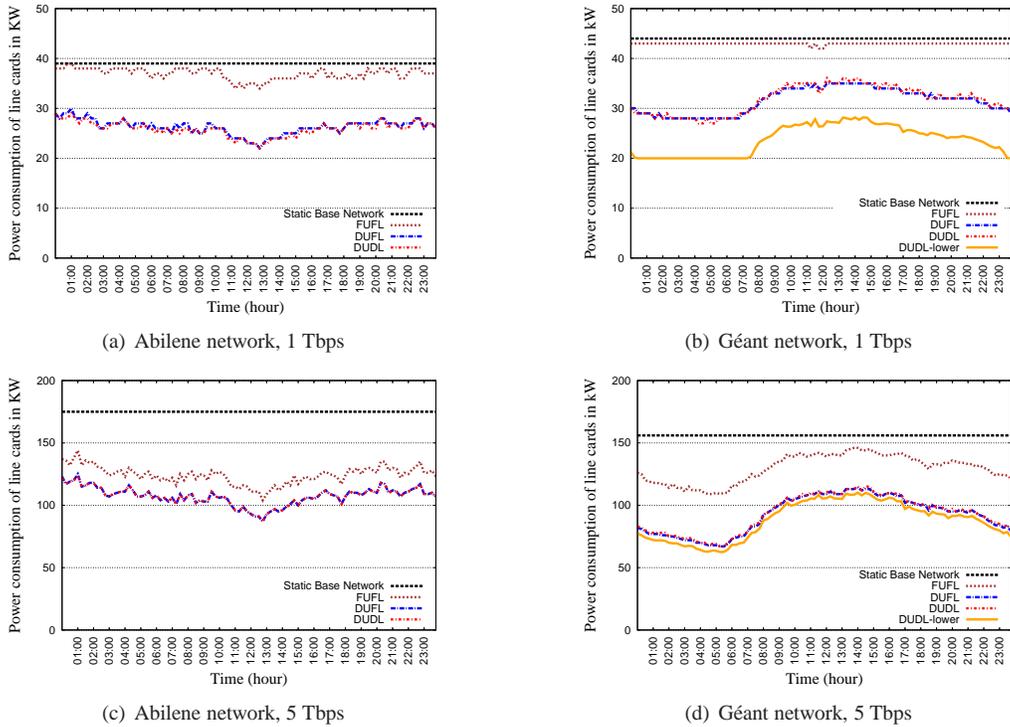


Figure 9: The results are independent of the network topology. The figures show the power consumption over time with the three approaches on the Géant and Abilene network with measured traffic demands, scaled to 1 Tbps, 5 Tbps maximum total demand, every 15 minutes of a day.

accordingly (FUFL) may bring substantial savings in power consumption. We observed however that the success of the latter simple strategy depends on the capacity of a WDM channel compared to the size of the demands as well as on the regional distribution of the demand. Given a constant lightpath capacity, the benefit of FUFL increases with increasing demands. Given the same lightpath capacity, the same total traffic and the same dynamics over time, less energy can be saved with FUFL under (non-realistic) evenly distributed demands over space than under demands with distribution originating from measurements.

Limitations and future areas of interest: In order to make our work as clear as possible, we summarize the limitations of our models. This can be helpful in further research to make even more accurate estimations of the potential energy savings.

First, despite using a sophisticated mathematical model, we did not find optimal solutions for some instances (especially DUDL), and reported the (relatively small) optimization gaps. The computational challenge is especially high, since one instance of DUFL and DUDL requires to solve one MILP for each considered point in time. We cov-

ered different time scales of the traffic demands in this work. It might be interesting to reduce the time granularity of the traffic matrices to check the influence of short-term traffic fluctuations of power consumption in backbone networks.

Second, our models assume a split of IP traffic demands over multiple parallel paths. This is a strong assumption, as multi-path routing is normally not enabled in today's routers. MPLS allows this kind of traffic engineering, but the label switched paths (LSP) are not frequently reconfigured today, either. Since single-path routing may reduce the utilization of lightpaths due to coarse granularity of demand values, DUDL may turn out to benefit more from its additional flexibility in the WDM layer, and outperform DUFL in terms of power consumption.

Wavelength assignment strategies are not integrated in the mathematical models. Since fibers rarely get highly utilized in the performed case studies we do not expect a substantial influence of this issue on the presented results. The situation might change in 40-channel DWDM systems or if demands increase beyond 5 Tbps.

Furthermore, power consumption in the WDM

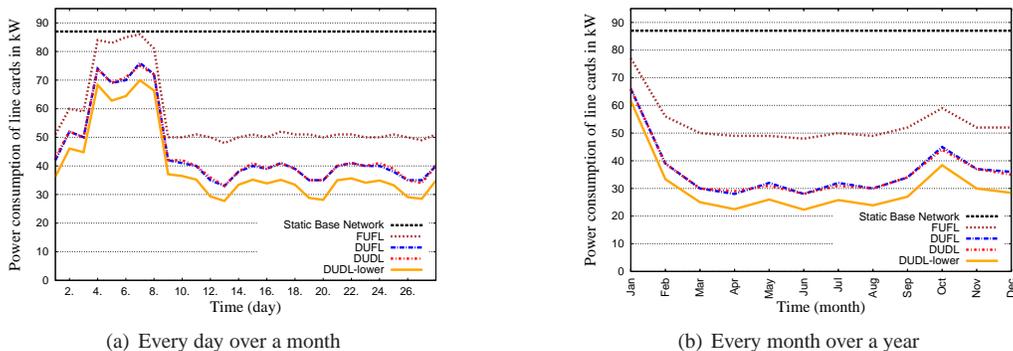


Figure 10: The results are independent of the time scale. The figures show the power consumption over time with FUFL, DUFL, and DUDL in the Germany17 network, DFN traffic, 3 Tbps, for a month and a year. The meaning of the curves is the same as in the 15-minute Fig. 6(b).

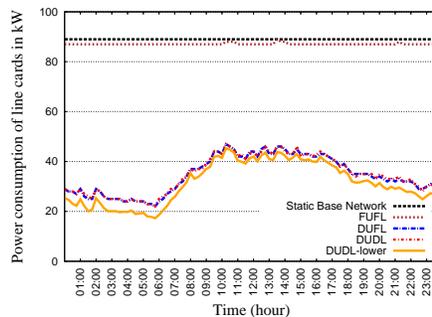


Figure 11: Power consumption over time with FUFL, DUFL, and DUDL in the Germany17 network, 3 Tbps, DWG traffic, 15 minutes over one day. The change of the spatial distribution of traffic affects the success of FUFL. Compare with Fig. 6(b).

layer can be incorporated in the objective function of DUFL and DUDL. Although we see some potential of energy saving by switching off optical devices (OLAs, regenerators, DGEs and parts of OXCs), our preliminary estimations indicate it to be much smaller than in the IP layer (which is in line with [28]). Realistic data about capacity and power consumption of OXCs would be necessary to proceed with this study.

Last but not least, we deliberately neglected operational issues in our estimation of the potential (maximum) of energy savings, as the goal of this paper was to perform a conceptual study on the maximum possible energy savings with the three rerouting mechanisms. Of course, in a practical implementation of these mechanisms, additional criteria have to be taken into account like QoS in terms of packet delay, jitter and packet loss, stability of transport protocols, durability of network components, time needed to reconfigure the network, etc. These implementational details were outside the scope of this paper.

Traffic engineering and reconfiguring the IP

routing is nowadays part of the daily business of network operators. Our work indicates that energy aspects should be considered already in the operational phase helping to save OPEX. It should also motivate equipment vendors to provide network elements with convenient and fast functionality to be switched on and off.

Acknowledgments

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Appendix A. Model variants for DUFL and DUDL

Complete mixed integer programming models to compute energy-minimal network configurations at time $t \in T$ using the two approaches DUFL and DUDL are presented in this section. Both models are simplifications of the original model (2) used to compute the base network in the sense that the solution space is restricted, which is achieved by fixing variables and adding constraints. Model (A.1) for DUFL and model (A.2) for DUDL are obtained from (2) by changing the objective, fixing variables y_e and x_i^n to the values of the base network, and adding constraint (A.1d) respectively (A.2e). It follows that the installation of fibers and IP routers is fixed to the configuration of the base network. We are only allowed to change the IP flow and the lightpath configuration (variables f_{ij}^k, f_{ji}^k, y_p). The new objective is to minimize the number of active lightpaths. In addition the right hand side of the demand constraints (A.1a) and (A.2a) now corresponds to the demands $d^{(t)}$ at time $t \in T$ which are by definition smaller than the maximum demands d used in (2).

$$\begin{aligned} \min \sum_{p \in P} y_p \\ \sum_{j \in V \setminus \{i\}} (f_{ij}^k - f_{ji}^k) = d_i^{k(t)}, \quad i \in V, k \in K \end{aligned} \quad (\text{A.1a})$$

$$\sum_{p \in P(i,j)} Cy_p - \sum_{k \in K} (f_{ij}^k + f_{ji}^k) \geq 0, \quad (i, j) \in V \times V \quad (\text{A.1b})$$

$$\sum_{p \in P_i} Cy_p \leq R_i^{base} - d_i^{(t)}, \quad i \in V \quad (\text{A.1c})$$

$$y_p \leq y_p^{base}, \quad p \in P \quad (\text{A.1d})$$

$$f_{ij}^k, f_{ji}^k \in \mathbb{R}_+, \quad y_p \in \mathbb{Z}_+ \quad (\text{A.1e})$$

Model (A.1) computes the energy-minimal network at time $t \in T$ using DUFL. By (A.1d) we cannot exceed the lightpath configuration in the base network, that is, we have to use existing ones or switch them off. In particular, if a path p is not used in the base network solution ($y_p^{base} = 0$) the corresponding path variable y_p is not generated for the DUFL model ($y_p = 0$). Also notice that the fiber constraints (2e) become redundant because of (A.1d). The number of wavelengths per fiber can only be reduced from the value in the base network solution. In fact there is no active physical capacity constraint for DUFL.

Model (A.2) computes the energy-minimal network at time $t \in T$ using DUDL. In contrast to

model (A.1) we may establish new lightpaths as long as the number of lightpaths ending at a node is not exceeding the same number in the base network. This guarantees that only the existing line cards are used. Notice that (A.2e) relaxes constraint (A.1d). Fiber constraints (A.2d) are not redundant for DUDL.

$$\begin{aligned} \min \sum_{p \in P} y_p \\ \sum_{j \in V \setminus \{i\}} (f_{ij}^k - f_{ji}^k) = d_i^{k(t)}, \quad i \in V, k \in K \end{aligned} \quad (\text{A.2a})$$

$$\sum_{p \in P(i,j)} Cy_p - \sum_{k \in K} (f_{ij}^k + f_{ji}^k) \geq 0, \quad (i, j) \in V \times V \quad (\text{A.2b})$$

$$\sum_{p \in P_i} Cy_p \leq R_i^{base} - d_i^{(t)}, \quad i \in V \quad (\text{A.2c})$$

$$\sum_{p \in P: e \in p} y_p \leq B y_e^{base}, \quad e \in E \quad (\text{A.2d})$$

$$\sum_{p \in P_i} y_p \leq \sum_{p \in P_i} y_p^{base}, \quad i \in V \quad (\text{A.2e})$$

$$f_{ij}^k, f_{ji}^k \in \mathbb{R}_+, \quad y_p \in \mathbb{Z}_+ \quad (\text{A.2f})$$

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